

## Numerical modelling of the reinforced concrete influence on a combined system of tunnel support

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### Abstract

The paper presents the experimental, laboratory determined rheological-dynamic analysis of the properties of fiber reinforced concrete, which was then utilized to show nonlinear analysis of combined system of tunnel support structure. According to the performed experiments and calculations, different processes of destructive behavior of tunnel lining were simulated in combination with elastic and elastic-plastic behavior of materials taking into account the tunnel loading, the interaction between the fiber reinforced concrete and soil, as well as the interaction between the fiber reinforced concrete and the inner lining of the tunnel.

**Key words:** reinforced concrete, nonlinear analysis, combined system of the tunnel

## 1 Introduction

Fiber Reinforced Concrete (FRC) is a composite material with a cementitious matrix and discontinuous reinforcement (the fibers) that may be made of metal, glass or synthetic materials. After almost four decades of research, mechanical properties of FRC are well known and standards for material characterization are widely available, and design guidelines have been recently proposed by RILEM. Among the structural applications of FRC, there is a growing interest to be used with the tunnel structures, where steel fibers may substitute conventional reinforcement concrete partially or totally.

The structural behavior of tunnel structures is numerically simulated with finite element analysis based on nonlinear fracture mechanics. The excavated Klačnice tunnel at the motorway E661 in Bosnia and Herzegovina has a diameter of about 5,85 m, and with the length of 477 m is located about 11 to 21 m below the surface. The study showed that the lining of conventional reinforced concrete can be replaced by FRC, having suitable thickness, with minimal total displacement. After the experimental characterization of the mechanical properties of Steel Fiber Reinforced Concrete (SFRC), FEM (Finite Element Method)

analysis allowed to study the structural behavior of the tunnel lining with different types of reinforcement under significant loading conditions.

## 2 Materials

The experimental characterization of the material properties of SFRC was performed on a concrete matrix used for the Klačnice tunnel. SFRC was made with cement CEM I 42.5 R, a rounded shape natural river gravel having maximum diameter of 12 mm. Its composition is summarized in Table 1.

Table 1: The percentage content of the aggregate used

Fraction	Percentage of passage on sieve (mm)											
	0,125	0,25	0,5	0,71	1	2	4	8	11,2	16	22,4	31,5
0/4 mm	1	5	30	45	55	80	95	100	100	100	100	100
4/8 mm	0	0	0	0	0	0	4	95	100	100	100	100
8/16 mm	0	0	0	0	0	0	0	2	47	100	100	100

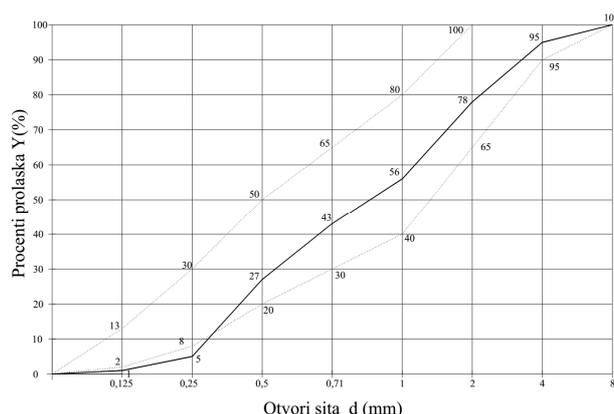


Figure 1: Granulometric curve aggregate fractions used for samples preparation

Within the experimental work, the basic properties and characteristics of the applied types of fibers were examined in laboratory (Table 2). The used steel fibers are made of pure steel, as well as mixtures of steel and aluminum. This feature of the non-uniformity of the applied fiber materials influenced the final properties of the fibers, which is evident from Table 2.

Table 2: Characteristics of applied steel fibers within the experiment

Properties	L=50	L=31	L=25
Shape			
Length (mm)	50	31	25
Diameter (mm)	0,75	0,75	0,75
Ratio factor L/D	67	41	34
Density (kg/m <sup>3</sup> )	7100	7350	7400
Tensile strength (MPa)	1150	1250	1300

### 3 Results of the experimental research

#### 3.1 Modulus of elasticity

The paper gives an overview of the determination of the modulus of elasticity of a cylindrical sample. The procedure is repeated in a series of three samples, and then the mean value of the elasticity module is taken.

Table 3: Determination of elasticity modulus of a cylindrical fiber reinforced concrete sample, measuring 150x300 mm, 2% of steel fibers L/D = 50/0,75

Modulus of elasticity E - sample number 1, Etalon					
Measuring place dilatation $10^{-3}$ (mm)	Force (kN)				
1	0	20	140	240	460
2	0	4	45		
3	0	4	15		
4	0	1	21		
5	0	1	4		
6	0	0	3		
1		18	38		
2		3	18		
3		1	19		
4		1	5		
5		0	4		
6		0	1		
1		9	35	90	200
2		7	16	30	65
3		0	15	50	110
4		2	3	7	20
5		0	2	5	20
6		0	1	2	5

Based on the performed tests, the mean values of the elasticity modules E are calculated for standard samples as well as for micro-reinforced concrete samples with different content of steel fiber with the shape factor L/D = 50/0,75 (fiber content of 1%, 2% and 3%).

Elasticity modules E are calculated through the following equation:

$$E = \Delta\sigma / \Delta\varepsilon \quad (1)$$

where:

$\Delta\sigma = \sigma_g - \sigma_d$  ( $\sigma$  - tensile stress);

$\sigma_g = f_p/3$  (the upper limit of the selected tensile strength)

$\sigma_d = 0,5$  MPa (the lower limit of the selected tensile strength);

$\Delta\varepsilon$  - the difference in the mean values of the dilations corresponding to  $\sigma_g$  and  $\sigma_d$ ;

$f_p$  - the pressure at which the sample breaks.

Figure 2. presents results of the rheological-dynamic model of material behavior in the standard concrete cylinder (300 x 150 mm) on the basis of the experimental data from Table 4. As visible, with the increase of fibers quantity the Poisson's coefficient ( $\mu$ ) decreases. Further, on the basis of the tests carried out, this means that the composite material, such as FRC, is a crude material in comparison with the standard concrete, and therefore the FRC has a higher deformability. This is a very important fact that needs to be emphasized when analyzing FRC. In terms of the  $\sigma$ - $\varepsilon$  diagram, deformation at the compressive strength  $\varepsilon_{fc}$  as well as the ultimate deformation  $\varepsilon_{ult.}$  is important. Pressure strength ( $f_c$ ) and proper deformation are consistent with all four concrete samples with experimental data. It is usual to perform quasi-static analysis of these diagrams and fracture energy, i.e. pressure toughness ( $G_C$ ) Also, the minimum coefficient of fracture ( $f_c/G_C$ ) determines the most favorable mix of concrete in the cylinder.

Table 4: Results of modulus of elasticity of standard and FRC concrete (L/D = 50/0,75)

1. Characteristics of the sample of concrete/etalon without fiber:

$$F_{c,28} = 37,60 \text{ Mpa}$$

$\rho$ (kg/m <sup>3</sup> )	$E_h$ (Mpa)	$E_d$ (Mpa)	$\mu$	$\varepsilon$ (mm)
2195,38	19917,05	24877,312	0,188	0,003

2. Characteristics of the sample of FRC with fiber content:

$$V_f = 1\% \text{ in } 1 \text{ m}^3 \text{ of concrete}$$

$$F_{c,28} = 38,00 \text{ Mpa}$$

$\rho$ (kg/m <sup>3</sup> )	$E_h$ (Mpa)	$E_d$ (Mpa)	$\mu$	$\varepsilon$ (mm)
2210,16	20879,16	26079,95	0,1685	0,0033

3. Characteristics of the sample of FRC with fiber content:

$$V_f = 2\% \text{ in } 1 \text{ m}^3 \text{ of concrete}$$

$$F_{c,28} = 38,7 \text{ Mpa}$$

$\rho$ (kg/m <sup>3</sup> )	$E_h$ (Mpa)	$E_d$ (Mpa)	$\mu$	$\varepsilon$ (mm)
2235,64	22061,4	27557,75	0,1565	0,0034

4. Characteristics of fibersample FRC with fiber content:

$$V_f = 3\% \text{ in } 1 \text{ m}^3 \text{ of concrete}$$

$$F_{c,28} = 40,00 \text{ Mpa}$$

$\rho$ (kg/m <sup>3</sup> )	$E_h$ (Mpa)	$E_d$ (Mpa)	$\mu$	$\varepsilon$ (mm)
2258,23	22182,95	27709,68	0,1373	0,0042

Note:  $V_f$  - content of fibers;  $F_{c,28}$  - pressure strength after 28 days

Table 5: Results of rheological-dynamic analysis of FRC (L/D = 50/0,75)

Concrete	$f_{c,28}$	$\varepsilon_{fc}$	$\varepsilon_{ult.}$	$G_C$ (N/mm)	$f_c/G_C$
Etalon	37,6	0,003	0,004794	21,0711	1,784
$V_f = 1\%$	38,0	0,0033	0,004979	20,0526	1,895
$V_f = 2\%$	38,7	0,0034	0,004954	19,1411	2,022
$V_f = 3\%$	40,0	0,0042	0,005791	20,3057	1,970

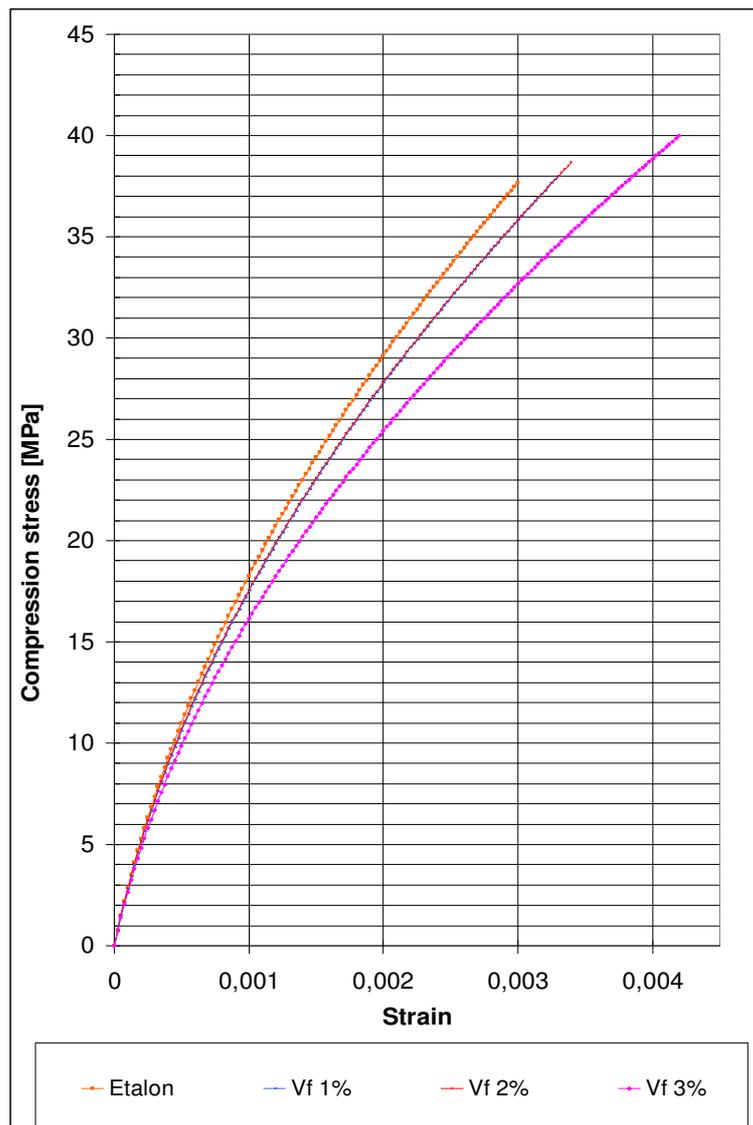


Figure 2: Graphical representation of the rheology-dynamic model for fibers  $L/D = 50/0,75$

### 3.2 Tensile Strength Testing

Although the tensile strength of the concrete during tightening is considerably less than the compressive strength of the concrete, the knowledge of the tensile strength of the concrete during tension is useful in determining when the cracks will begin to develop. Cracks represent the lack of concrete which significantly affects the physical and mechanical properties of concrete as well as the durability of concrete structures. The tensile strength depends primarily on the type of aggregate, the content of cement, the water-cement factor, the type and quantity of fibers, the shape of the fibers, the technological procedures for the preparation, installation and care of concrete. Results of testing tensile strength are given in Table 6.

Table 6: Tensile strength results depending on the fiber types and amount

Characteristics of used fibers				Fiber content %	Tensile strength		
Fiber shape	L [mm]	D [mm]	L/D		Etalon (concrete without fiber) [Mpa]	Micro- reinforced concrete [Mpa]	Increase in tensile strength %
	50	0,75	67	1	6,0	11,59	93,16
	50			2	6,0	12,0	100
	50			3	6,0	11,7	95
	31	0,75	41	1	6,0	9,5	58,33
	31			2	6,0	9,4	56,66
	31			3	6,0	9,4	56,66
	25	0,75	25	1	6,0	7,8	30
	25			2	6,0	7,9	31,66
	25			3	6,0	8,0	33,33

### 3.3 Bending strength

The influence of steel fibers on the bending strength of the FRC is much higher than on the compressive strength and tensile strength. Usually, two strengths are provided for bending elements. The first called “strength at first cracking” corresponds to the load diagram - the angle of the point to which the diagram is approximately linear (point A, Figure 3.), and the second, called “boundary strength”, corresponds to the maximum tension achieved, in the Figure 3. This is the point C which corresponds to the maximum load.

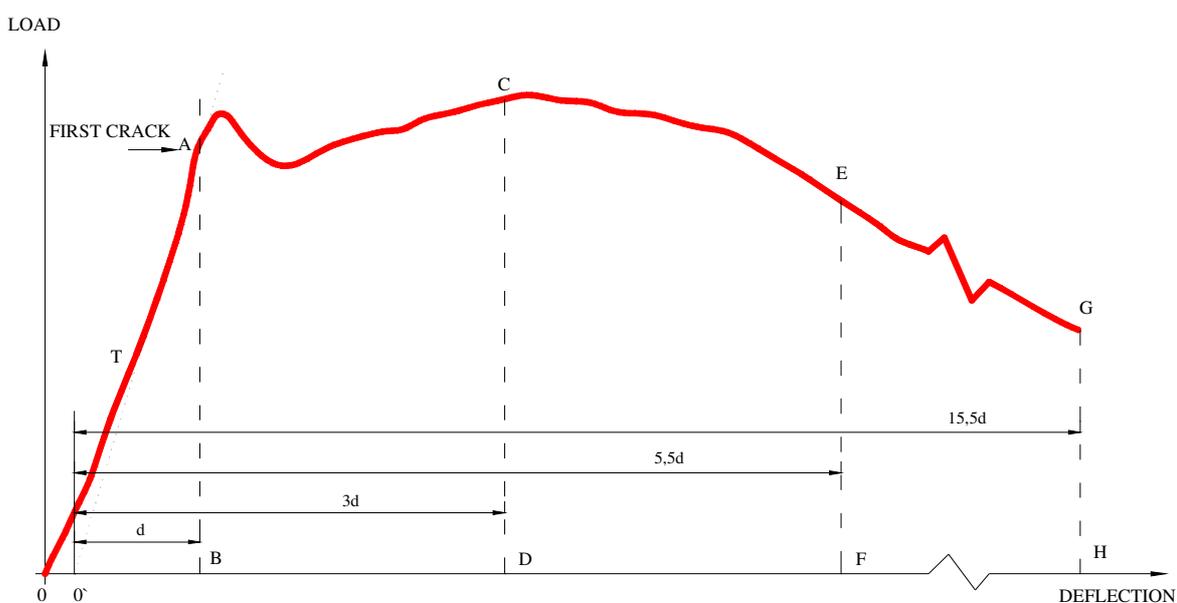


Figure 3: Diagram load - deflection for FRC, beam 100x100x400 mm

## 4 Description of the applied model for tunnel structure

Numerical methods, in particular FEM, represent a valuable contribution to a much more accurate estimation of the tensile and displacement in tunnels and surrounding rock masses. But the FEM is useful only if a numerical method is applied that correctly describes the natural behavior of the rock mass.

Choosing the model of the tunnel structure, the quality of the rock mass, the degree of variability and quality along the tunnel are respected. Construction technology and the height of the overhangs also have an impact on this choice. The cross-section is a complex figure in the shape of figure of 5,85 m, a protruding height of 2,00 m and a foot bucket that closes the entire contour. This type of tunnel extends through the geotechnical model A of the tunnel with the characteristics given in a Table 7.

Table 7: Model A for Coulomb-Mohr

Geotechnical data:	diabase formation
$\gamma$ (kN/m <sup>3</sup> )	25
$\phi$ (°)	25
E (Mpa)	2000
$\nu$ (-)	0,28
c (Mpa)	0,20
D (Mpa)	120

### 4.1 Introductory notes for the numerical model

A model of a traffic tunnel was adopted for numerical testing of the comparison of the behavior of the excavation insurance (Figure 4). The shown comparison is the behavior of the excavating contour:

- using a conventional concrete class 30 reinforced with two-layer steel grid;
- using FRC class 38.7 reinforced steel fibers with curved ends and shape factor  $L/D = 50/0,75$  and the amount of fiber present 2% compared to the total concrete mixture.

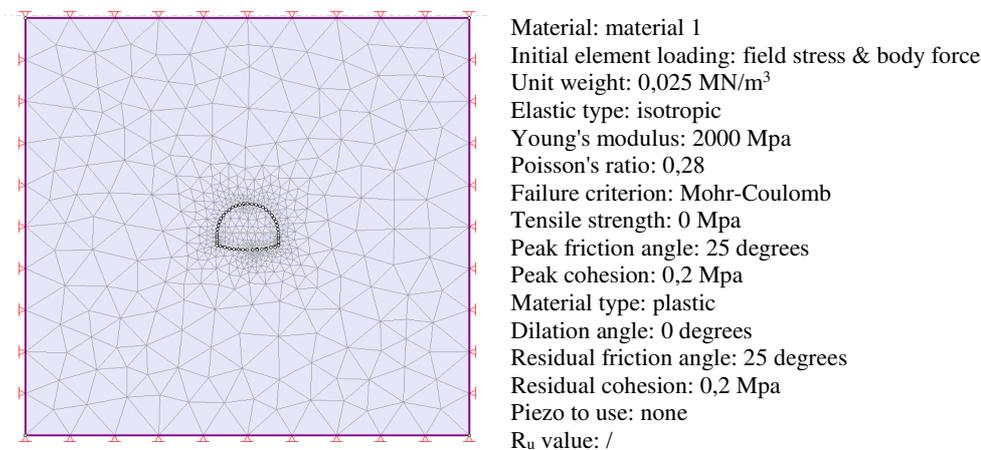


Figure 4: Basic model of tunnel and the surrounding rock geotechnical characteristics

The aim of this numerical analysis was to show the behavior of the rock mass around the excavation in the case of applying the FRC with characteristic  $L/D = 50/0,75$  with emphasis on the substantially increased tensile strength of this concrete and for all other parameters of the same for both cases: geotechnical characteristics of the rock mass, load during phase of excavation and compressive strength of basic material e.g. reinforced concrete. Passive anchors are not installed because they are not important for this study.

The reinforced concrete lining is treated as a shaft element because it is capable of reinforcing the normal forces, transverse forces and bending moments.

In the software PHASE2v6 total displacements for the two phases of the excavation were compared, depending on the thickness of the tunnel lining for reinforced concrete and fiber reinforced concrete (Table 8).

Table 8:  $\max U_{\text{tot}}$  (maximum displacement) for models processed in PHASE2v6 depending on the thickness of the tunnel lining D

D (cm)	$\max U_{\text{tot}}$	
	1 <sup>st</sup> phase	2 <sup>nd</sup> phase
RC 15	0,00661257	0,00607221
RC 20	0,00661257	0,00605811
RC 25	0,00667319	0,00604121
FRC 15	0,00654235	0,00608391
FRC 20	0,00661257	0,00605811
FRC 25	0,00667319	0,00604121

## 5 Conclusion

The use of FRC with steel fibers, with curved ends, and a shape factor  $L/D = 50/0,75$  in an amount of 2% in weight of concrete gives excellent results in the tunnel structure calculation. In doing so, the total displacement of the FRC tunnel coating corresponds to the total displacement of the tunnel lining of reinforced concrete. This demonstrates the possibility of using the FRC in the calculation of underground objects instead of reinforced concrete coating, with one great note that the FRC manufacturing technology and the homogeneity of the concrete mix represent a key factor for the good indicators and properties of the tested micro-reinforced composite.

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