CHEMICALLY REACTING IONIZED RADIATIVE FLUID FLOW THROUGH AN IMPULSIVELY STARTED VERTICAL PLATE WITH INDUCED MAGNETIC FIELD

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Numerical studies have been performed to examine the chemically reacting ionized fluid flow through a vertical plate with induced magnetic field. This study is performed for the cooling problem. To obtain the non-dimensional non-similar momentum, the induced magnetic field, energy and concentration equations, usual non-dimensional variables have been used. The numerical solutions for the velocity fields, induced magnetic fields, temperature distribution as well as concentration distribution are obtained for associated parameters using the explicit finite difference method. The local and average shear stresses, current densities, Nusselt number as well as the Sherwood number are also investigated. The obtained results are discussed with the help of graphs to observe effects of various parameters entering into the problem. Also the stability conditions of the explicit finite difference method are analyzed. Finally, a qualitative comparison of the present results with previously published results has been made.

Key words: boundary layer, radiative flow, strong magnetic field, ionized gas, flow fields.

1. Introduction

The effects of ionized fluid flow on MHD boundary layer flow have become important in several industrial processes, scientific and engineering fields. It has been found by Cowling [1] that the ionized fluid has two distinct effects. The first effect - electric currents can flow in an ionized fluid because of relative diffusion of the ionized gas and electrons due to agencies of electric forces. The second effect depends wholly on the magnetic field. The convection flow is often encountered in nuclear reactors or in the study of planets and stars. There are many engineering problems which are susceptible to ionized fluid flow analysis. It is useful in astrophysics because much of the universe is filled with widely spaced charged particles and permeated by magnetic fields and so the continuum assumption becomes applicable. In many engineering applications, combined heat and mass transfer play an important role in fluids condensing or boiling at a solid surface. The combined heat and mass transfer are due to buoyancy forces caused by thermal and mass diffusions. Condensing and boiling are characteristic for many separation processes in chemical engineering.

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such as drying, evaporation, distillation, condensation, rectification and absorption of a fluid. The combined buoyancy effects of thermal and mass diffusions on natural convection flow have been investigated by Gebhart and Pera [2]. The studies of MHD incompressible viscous flows with Hall currents have grown considerably because of their engineering applications to the problems of Hall accelerators, MHD generators, constructions of turbines and centrifugal machines, as well as flight magnetohydrodynamics. The effects of Hall currents on free convective flow through a porous medium bounded by an infinite vertical plate have been studied by Ram [3], when a strong magnetic field is imposed in a direction which is perpendicular to the free stream and makes an angle to the vertical direction. The Hall effects on an unsteady MHD free convective heat and mass transfer flow through a porous medium near an infinite vertical porous plate with constant heat flux and variable suction have been analyzed by Sattar and Alam [4].

The interaction of buoyancy with thermal radiation has studied extensively greatly during the last decade due to its importance in many practical applications. The combined effects of gas radiation and magnetic field on the mixed convection flow from a permeable vertical plate have been investigated by Aydin and Kaya [5] with the extension of MHD mixed convection flow about a permeable vertical plate.

The Soret and Dufour effects have been found to influence the flow field in mixed convection boundary layer over a vertical surface embedded in a porous medium. The effect of thermal radiation, Hall currents, Soret and Dufour effects on MHD flow by mixed convection over a vertical surface in porous media has been studied by Shateyi et al. [6]. The effects of Soret, Dufour numbers, chemical reaction, thermal radiation and volumetric heat generation/absorption on mixed convection stagnation point flow on an isothermal vertical plate in porous media have been analyzed by Olanrewaju and Gbadeyan [7]. Recently, the effects of Soret and Dufour on unsteady MHD flow by mixed convection over a vertical surface in porous media with internal heat generation, chemical reaction and Hall current have been investigated by Aurangzaib and Shafie [8]. Ahmed and Alam [9] solved the Aurangzaib and Shafie [8] model by the implicit finite difference method.

All the above papers concentrated on MHD free convection heat and mass transfer flow of an incompressible viscous fluid past a continuously moving surface under only the action of a transverse magnetic field with or without thermal diffusion, thermo and chemical reaction for a small magnetic Reynolds number. If the magnetic Reynolds number of the flow is not taken to be small enough and the flow under the action of a strong magnetic field that induced another magnetic field is of great interest in geophysics and astrophysics. The steady combined heat and mass transfer flow with an induced magnetic field has been analytically analyzed by Chaudhary and Sharma [10]. The unsteady heat and mass transfer by mixed convection flow from a vertical porous plate with an induced magnetic field, constant heat and mass fluxes has been investigated by Alam et al. [11]. The numerical simulation and stability on MHD free convective heat and mass transfer unsteady flow through a porous medium in a rotating system with an induced magnetic field has been investigated by Haque et al. [12]. For an unsteady two dimensional case, with Hall effect, chemical reaction, thermal radiation, thermal-diffusion, diffusion thermo, induced magnetic field and inclined uniform magnetic field the above problem becomes more complicated. These types of problems play a special role in nature, in many separation processes such as isotope separation, in mixtures between gases, in many industrial applications such as solidification of binary alloy as well as in astrophysical and geophysical engineering.

Hence our aim of this research is to extend the work of Ahmed and Alam [9] with an induced magnetic field. The problem has been solved by the explicit finite difference method (Carnahan et al. [13]). The governing equations involved in this problem have been transformed into dimensionless non-similar coupled partial differential equations by usual transformations. Finally, a comparison of the present results with the results of Haque et al. [12]) has been made.

2. Mathematical model of the flow

A flow model of an unsteady chemically reacting ionized mixed convective heat and mass transfer flow of an electrically conducting incompressible viscous fluid past an electrically nonconducting semi-infinite vertical porous plate with thermal diffusion and diffusion thermo effect is considered. It
Chemically reacting ionized radiative fluid flow through ... considered that the effects of Joule heating, radiation and heat source or absorption are considered. The positive $x$ coordinate is measured along the plate in the direction of fluid motion and the positive $y$ coordinate is measured normal to the plate. The leading edge of the plate is taken as coincident with the $z-$ axis. Initially, it is considered that the plate as well as the fluid are at the same temperature $T(=T_\infty)$ and the concentration level $C(=C_\infty)$. Also, it is assumed that the fluid and the plate are at rest after that the plate is moving with a constant velocity in its own plane. Instantaneously at time $t > 0$, the temperature of the plate and species concentration are raised to $T_w$ and $C_w$, respectively, which are thereafter maintained constant, where $T_w, C_w$ are temperature and species concentration at the wall and $T_\infty, C_\infty$ are the temperature and concentration of the species outside the plate respectively. The physical configuration of the problem is shown in Fig.1.

A strong uniform magnetic field $H_0$ can be taken as $(0, \lambda H_0, \sqrt{1-\lambda^2} H_0)$ where $\lambda = \cos \alpha$ is applied in a direction that makes an angle $\alpha$ with the normal to the considered plate. Thus if $\lambda = 1$, the imposed magnetic field is parallel to the $y-$ axis and if $\lambda = 0$, then the magnetic field is parallel to the plate. The magnetic Reynolds number of the flow is not taken to be small enough, the induced magnetic field is not negligible. The divergence equation $\nabla \cdot H = 0$ of Maxwell’s equation for the magnetic field gives $H_y = \lambda H_0$. We use the relation $\nabla \cdot J = 0$ for the current density $J = (J_x, J_y, J_z)$ where $J_y = \text{constant}$. Since the plate is non conducting, $J_y = 0$ at the plate and hence zero everywhere. Within the framework of the above stated assumptions, the equations relevant to the two-dimensional problem are governed by the following system of coupled non-linear partial differential equations.

Continuity equation
\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 . \quad (2.1)
\]

Momentum equations
\[
\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = \nu \frac{\partial^2 u}{\partial y^2} + g \beta_T (T - T_\infty) + g \beta_C (C - C_\infty) - \frac{\mu}{\rho k_l} u + \frac{\mu \lambda H_0}{4 \pi \rho} \frac{\partial H_z}{\partial y}, \quad (2.2)
\]
\[
\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} = \nu \frac{\partial^2 w}{\partial y^2} - \frac{\mu}{\rho k_l} w + \frac{\mu \lambda H_0}{4 \pi \rho} \frac{\partial H_z}{\partial y}. \quad (2.3)
\]
Magnetic induction equations
\[
\frac{\partial H_x}{\partial t} + v \frac{\partial H_x}{\partial y} = \eta \frac{\partial^2 H_x}{\partial y^2} + H_x \frac{\partial u}{\partial x} + \lambda \beta_e \eta \frac{\partial^2 H_z}{\partial y^2}, \quad (2.4)
\]
\[
\frac{\partial H_z}{\partial t} + v \frac{\partial H_z}{\partial y} = \eta \frac{\partial^2 H_z}{\partial y^2} + H_x \frac{\partial w}{\partial x} + \lambda \beta_e \eta \frac{\partial^2 H_z}{\partial y^2}, \quad (2.5)
\]
Energy equation
\[
\frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \kappa \frac{\partial^2 T}{\partial y^2} + \frac{D k_i}{c_i c_p} \frac{\partial^2 C}{\partial y^2} + \frac{1}{16 \pi^2 \rho c_p \sigma} \left( \frac{\partial H_z}{\partial y} \right)^2 + \left( \frac{\partial H_x}{\partial y} \right)^2 + \frac{1}{\rho c_p} \frac{\partial q_r}{\partial y} + \frac{Q}{\rho c_p} (T - T_\infty)^p. \quad (2.6)
\]
Concentration equation
\[
\frac{\partial C}{\partial t} + u \frac{\partial C}{\partial x} + v \frac{\partial C}{\partial y} = D \frac{\partial^2 C}{\partial y^2} + \frac{D k_i}{T_m} \frac{\partial^2 T}{\partial y^2} - k_0 \frac{C - C_\infty}{C_\infty}. \quad (2.7)
\]
In addition, the boundary conditions for the model are
\[
u = U_\infty, \quad v = 0, \quad w = 0, \quad H_x = H_w, \quad H_z = 0, \quad T = T_w, \quad C = C_w \quad \text{at} \quad y = 0, \quad (2.8)
\]
\[
u = 0, \quad v = 0, \quad w = 0, \quad H_x = 0, \quad H_z = 0, \quad T \to 0, \quad C \to 0 \quad \text{as} \quad y \to \infty
\]
where \( u, v \) and \( w \) are the \( x, y \) and \( z \) components of the velocity vector, \( H_x \) and \( H_z \) are the \( x \) and \( z \) components of the magnetic induction vector, \( H_0 \) is the uniform magnetic field, \( H_w \) is the induced magnetic field at the wall, \( g \) is the local acceleration due to gravity, \( \beta_T \) is the thermal expansion coefficient; \( \beta_C \) is the concentration expansion coefficient, \( \nu \) is the kinematics coefficient of viscosity, \( \mu \) is the fluid viscosity, \( \mu_e \) is the magnetic permeability, \( \rho \) is the density of the fluid, \( \kappa \) is the thermal conductivity, \( c_p \) is the specific heat at the constant pressure, \( k_0 \) is the rate of chemical reaction and \( D \) is the coefficient of mass diffusivity, \( k_i \) is the thermal diffusion ratio, \( c_s \) is the concentration susceptibility, respectively. Here \( p \) and \( q \) are considered as positive constant. The radiative heat flux \( q_r \) is described by the Rosseland approximation (Brewster [14]) such that \( q_r = -\frac{4 \sigma^* T^4}{3 k^*} \), where \( \sigma^* \) and \( k^* \) are the Stefan-Boltzmann constant and the mean absorption coefficient, respectively. If the temperature difference within the flow is sufficiently small so that \( T^4 \) can be expressed as a linear function after using Taylor series to expand
\( T^4 \) about the free stream temperature \( T_\infty \) and neglecting higher-order terms, then we have the following approximation: \( T^4 \approx 4T_\infty^3T - 3T_\infty^4 \).

3. Mathematical formulation

Since the solutions of the governing Eqs (2.1)-(2.7) under the boundary conditions (2.8) will be based on the finite difference method it is required to make the said equations dimensionless. For this purpose, the following dimensionless quantities are introduced

\[
X = \frac{xU_\infty}{\nu}, \quad Y = \frac{yU_\infty}{\nu}, \quad U = \frac{u}{U_\infty}, \quad V = \frac{v}{U_\infty}, \quad W = \frac{w}{U_\infty}, \quad \tau = \frac{tU_\infty^2}{\nu},
\]

\[
H_j = \sqrt{\frac{\mu_e}{\rho} \frac{H_x}{U_\infty}}, \quad H_3 = \sqrt{\frac{\mu_e}{\rho} \frac{H_z}{U_\infty}}, \quad \bar{T} = \frac{T - T_w}{T_w - T_\infty}, \quad \bar{C} = \frac{C - C_\infty}{C_w - C_\infty}.
\]

Using these relations, in Eqs (2.1)-(2.7) and corresponding boundary conditions (2.8) after simplification, the following nonlinear-coupled partial differential equations in terms of dimensionless variables are obtained

\[
\frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} = 0, \quad (3.1)
\]

\[
\frac{\partial U}{\partial \tau} + U \frac{\partial U}{\partial X} + V \frac{\partial U}{\partial Y} = \frac{\partial^2 U}{\partial Y^2} + \text{Gr} \bar{T} + \text{Gm} \bar{C} - KU + \lambda M \frac{\partial H_j}{\partial Y}, \quad (3.2)
\]

\[
\frac{\partial W}{\partial \tau} + U \frac{\partial W}{\partial X} + V \frac{\partial W}{\partial Y} = \frac{\partial^2 W}{\partial Y^2} - KW + \lambda M \frac{\partial H_3}{\partial Y}, \quad (3.3)
\]

\[
\frac{\partial H_j}{\partial \tau} + V \frac{\partial H_j}{\partial Y} = \frac{1}{P_m} \frac{\partial^2 H_j}{\partial Y^2} + H_j \frac{\partial U}{\partial X} + \lambda M \frac{\partial U}{\partial Y} - \frac{\lambda \mu_e}{P_m} \frac{\partial^2 H_3}{\partial Y^2}, \quad (3.4)
\]

\[
\frac{\partial H_3}{\partial \tau} + V \frac{\partial H_3}{\partial Y} = \frac{1}{P_m} \frac{\partial^2 H_3}{\partial Y^2} + H_3 \frac{\partial W}{\partial X} + \lambda M \frac{\partial W}{\partial Y} + \frac{\lambda \mu_e}{P_m} \frac{\partial^2 H_j}{\partial Y^2}, \quad (3.5)
\]

\[
\frac{\partial \bar{T}}{\partial \tau} + U \frac{\partial \bar{T}}{\partial X} + V \frac{\partial \bar{T}}{\partial Y} = \left( \frac{1 + R}{\text{Pr}} \right) \frac{\partial^2 \bar{T}}{\partial Y^2} + \text{Du} \frac{\partial^2 \bar{C}}{\partial Y^2} + \frac{\text{Ec}}{P_m} \left( \frac{\partial H_1}{\partial Y} \right)^2 + \left( \frac{\partial H_j}{\partial Y} \right)^2 + \beta \bar{T}^p, \quad (3.6)
\]

\[
\frac{\partial \bar{C}}{\partial \tau} + U \frac{\partial \bar{C}}{\partial X} + V \frac{\partial \bar{C}}{\partial Y} = \frac{1}{\text{Sc}} \frac{\partial^2 \bar{C}}{\partial Y^2} + \text{Sr} \frac{\partial^2 \bar{T}}{\partial Y^2} - \gamma \bar{C}^q. \quad (3.7)
\]

The boundary conditions are

\[
U = 1, \quad V = 0, \quad W = 0, \quad H_j = \sqrt{\frac{\mu_e}{\rho} \frac{H_w}{U_\infty}} = l \text{ (say)}, \quad H_3 = 0, \quad \bar{T} = 1, \quad \bar{C} = 1, \quad \text{at} \quad Y = 0, \quad (3.8)
\]

\[
U = 0, \quad V = 0, \quad W = 0, \quad H_j = 0, \quad H_3 = 0, \quad \bar{T} \to 0, \quad \bar{C} \to 0 \quad \text{as} \quad Y \to \infty
\]
where $\tau$ represents the dimensionless time, $X$ and $Y$ are the dimensionless Cartesian coordinates, $U$, $V$ and $W$ are the dimensionless velocity components, $H_1$ and $H_3$ are the dimensionless primary and secondary induced magnetic field, $\bar{T}$ is the dimensionless temperature, $\bar{C}$ is the dimensionless concentration, $\bar{U}$, $\bar{V}$ and $\bar{W}$ are the dimensionless velocity components, $\bar{1H}$ and $\bar{3H}$ are the dimensionless primary and secondary induced magnetic field, $T$ is the dimensionless temperature, $C$ is the dimensionless concentration, $\bar{U}_\infty$ is the dimensionless velocity at infinity, $\bar{T}_\infty$ is the dimensionless temperature at infinity, $\bar{C}_\infty$ is the dimensionless concentration at infinity, $\bar{U}^2$ is the dimensionless velocity at infinity, $\bar{T}^2$ is the dimensionless temperature at infinity, $\bar{C}^2$ is the dimensionless concentration at infinity, $\bar{1H}_\infty$ is the dimensionless primary induced magnetic field at infinity, $\bar{3H}_\infty$ is the dimensionless secondary induced magnetic field at infinity, $\bar{T}_\infty$ is the dimensionless temperature at infinity, $\bar{C}_\infty$ is the dimensionless concentration at infinity.

4. Shear stress, current density, Nusselt and Sherwood number

The quantities of chief physical interest are shear stress, current density, Nusselt number and Sherwood number. The following equations represent the local and average shear stress at the plate. Local shear stress in the $x$-direction, $\tau_{xL} = \mu_0 \left[ \frac{\partial u}{\partial y} \right]_{y=0}$ and average shear stress in the $x$-direction, $\tau_{xA} = \mu_0 \left[ \int_0^{\infty} \frac{\partial u}{\partial y} \right]_{y=0}$ are proportional to $\left( \frac{\partial U}{\partial Y} \right)_{Y=0}$ and $\int_0^{\infty} \left( \frac{\partial U}{\partial Y} \right)_{Y=0} dX$ are given respectively. The local shear stress in the $z$-direction, $\tau_{zL} = \mu_0 \left[ \frac{\partial w}{\partial y} \right]_{y=0}$ and average shear stress in the $z$-direction, $\tau_{zA} = \mu_0 \left[ \int_0^{\infty} \frac{\partial w}{\partial y} \right]_{y=0}$ which are proportional to $\left( \frac{\partial W}{\partial Y} \right)_{Y=0}$ and $\int_0^{\infty} \left( \frac{\partial W}{\partial Y} \right)_{Y=0} dX$ are given respectively. From the induced magnetic field, the effects of various parameters on the local and average current density have been investigated. The following equations represent the local and average current density at the plate: local current density in the $x$-direction, $\bar{j}_{xL} = \mu_0 \left[ \frac{\partial H_x}{\partial y} \right]_{y=0}$ and average current density in $x$-direction, $\bar{j}_{xA} = \mu_0 \left[ \int_0^{\infty} \frac{\partial H_x}{\partial y} \right]_{y=0}$ which are proportional to $\left( \frac{\partial H_x}{\partial Y} \right)_{Y=0}$ and $\int_0^{\infty} \left( \frac{\partial H_x}{\partial Y} \right)_{Y=0} dX$, respectively. The local current density in the $z$-direction, $\bar{j}_{zL} = \mu_0 \left[ \frac{\partial H_z}{\partial y} \right]_{y=0}$ and average current density in the $z$-direction, $\bar{j}_{zA} = \mu_0 \left[ \int_0^{\infty} \frac{\partial H_z}{\partial y} \right]_{y=0}$ which are proportional to $\left( \frac{\partial H_z}{\partial Y} \right)_{Y=0}$ and $\int_0^{\infty} \left( \frac{\partial H_z}{\partial Y} \right)_{Y=0} dX$, respectively.
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proportional to \( \left( -\frac{\partial H_3}{\partial Y} \right)_{Y=0} \) and \( \int_0^{100} \left( -\frac{\partial H_3}{\partial Y} \right)_{Y=0} dX \), respectively. From the temperature field, the effects of various parameters on the local and average heat transfer coefficients have been studied. The following equations represent the local and average heat transfer rate that is the well known Nusselt number, local Nusselt number, \( N_{u_L} = -\mu_0 \left( \frac{\partial T}{\partial Y} \right)_{y=0} \) and average Nusselt number, \( N_{u_A} = -\mu_0 \int_0^{100} \left( \frac{\partial T}{\partial Y} \right)_{y=0} dx \) which are proportional to \( \left( \frac{\partial T}{\partial Y} \right)_{y=0} \) and \( \int_0^{100} \left( \frac{\partial T}{\partial Y} \right)_{y=0} dX \), respectively. And from the concentration field, the effects of various parameters on the local and average mass transfer coefficients have been analyzed. The following equations represent the local and average mass transfer rate, that is the well known Sherwood number, local Sherwood number, \( S_{h_L} = -\mu_0 \left( \frac{\partial C}{\partial Y} \right)_{y=0} \) and average Sherwood number, \( S_{h_A} = -\mu_0 \int_0^{100} \left( \frac{\partial C}{\partial Y} \right)_{y=0} dx \) which are proportional to \( \left( \frac{\partial C}{\partial Y} \right)_{y=0} \) and \( \int_0^{100} \left( \frac{\partial C}{\partial Y} \right)_{y=0} dX \), respectively.

5. Numerical solutions

To solve the non-dimensional system by the explicit finite difference method, a set of finite difference equations. To obtain the difference equations the region of the flow is divided into a grid or mesh of lines parallel to the \( X \) and \( Y \) axes where the \( X \)-axis is taken along the plate and the \( Y \)-axis is normal to the plate.

![Fig.2. Explicit finite difference system grid.](image)

Here the plate of height \( X_{\text{max}} (= 100) \) is considered, i.e. \( X \) varies from \( 0 \) to \( 100 \) and \( Y_{\text{max}} (= 35) \) is assumed as corresponding to \( Y \to \infty \), i.e. \( Y \) varies from \( 0 \) to \( 35 \). There are \( m' (= 200) \) and \( n' (= 200) \)
grid spacing in the $X$ and $Y$ directions respectively as shown Fig.2. $\Delta X$, $\Delta Y$ are constant mesh sizes along the $X$ and $Y$ directions respectively and are taken as follows, $\Delta X = 0.5(0 \leq X \leq 100)$ and $\Delta Y = 0.175(0 \leq Y \leq 35)$ with the smaller time-step, $\Delta \tau = 0.005$. Let $U'$, $W'$, $H'_1$, $H'_3$, $\overline{T}$ and $\overline{C}$ denote the values of $U$, $W$, $H_1$, $H_3$, $\overline{T}$ and $\overline{C}$ at the end of a time-step, respectively. Using the explicit finite difference approximation, the system of partial differential Eqs (3.1)-(3.7) and the boundary conditions (3.8), we obtain an appropriate set of finite difference equations

\[
\frac{U'_r, j - U'_{r-1, j}}{\Delta X} + \frac{V'_{r, j} - V'_{r-1, j}}{\Delta Y} = 0, \quad (5.1)
\]

\[
\frac{U'_r, j - U'_{r-1, j}}{\Delta \tau} + \frac{U'_{r, j} - U'_{r-1, j}}{\Delta X} + \frac{V'_{r, j} - V'_{r-1, j}}{\Delta Y} = \frac{U'_{r, j+1} - 2U'_{r, j} + U'_{r, j-1}}{\Delta X^2} + \frac{V'_{r, j+1} - 2V'_{r, j} + V'_{r, j-1}}{\Delta Y^2} + \frac{\Delta \tau}{\Delta Y^2}
\]

\[
+Gr \overline{T}_{r, j} + Gm \overline{C}_{r, j} - KU'_{r, j} + \lambda M \frac{H'_{1r, j-1} - H'_{1r, j}}{\Delta Y}, \quad (5.2)
\]

\[
\frac{W'_{r, j} - W'_{r-1, j}}{\Delta X} + \frac{W'_{r, j} - W'_{r-1, j}}{\Delta X} + \frac{V'_{r, j} - V'_{r-1, j}}{\Delta Y} = \frac{W'_{r, j+1} - 2W'_{r, j} + W'_{r, j-1}}{\Delta X^2} + \frac{W'_{r, j+1} - 2W'_{r, j} + W'_{r, j-1}}{\Delta Y^2} + \frac{\Delta \tau}{\Delta Y^2}
\]

\[
-KW'_{r, j} + \lambda M \frac{H'_{3r, j-1} - H'_{3r, j}}{\Delta Y}, \quad (5.3)
\]

\[
\frac{H'_{1r, j}}{\Delta \tau} + V'_{r, j} \frac{H'_{1r, j-1} - H'_{1r, j}}{\Delta Y} = \frac{1}{P_m} \left( \frac{H'_{1r, j+1} - 2H'_{1r, j} + H'_{1r, j-1}}{\Delta Y^2} \right) + H'_{1r, j} \frac{U'_{r, j} - U'_{r-1, j}}{\Delta X} + \lambda M \frac{U'_{r, j+1} - U'_{r, j-1}}{\Delta X} + \frac{\lambda \beta_e}{P_m} \frac{H'_{1r, j+1} - 2H'_{1r, j} + H'_{1r, j-1}}{\Delta Y} + \frac{\lambda \beta_e}{P_m} \frac{H'_{3r, j+1} - 2H'_{3r, j} + H'_{3r, j-1}}{\Delta Y} \quad (5.4)
\]

\[
\frac{H'_{3r, j}}{\Delta \tau} + V'_{r, j} \frac{H'_{3r, j-1} - H'_{3r, j}}{\Delta Y} = \frac{1}{P_m} \left( \frac{H'_{3r, j+1} - 2H'_{3r, j} + H'_{3r, j-1}}{\Delta Y^2} \right) + H'_{3r, j} \frac{W'_{r, j} - W'_{r-1, j}}{\Delta X} + \lambda M \frac{W'_{r, j+1} - W'_{r, j-1}}{\Delta X} + \frac{\lambda \beta_e}{P_m} \frac{H'_{3r, j+1} - 2H'_{3r, j} + H'_{3r, j-1}}{\Delta Y} + \frac{\lambda \beta_e}{P_m} \frac{H'_{3r, j+1} - 2H'_{3r, j} + H'_{3r, j-1}}{\Delta Y} \quad (5.5)
\]

\[
\frac{T'_{r, j}}{\Delta \tau} + U'_{r, j} \frac{T'_{r, j} - T'_{r-1, j}}{\Delta X} + V'_{r, j} \frac{T'_{r, j+1} - T'_{r, j-1}}{\Delta Y} = \left( 1 + \frac{R}{Pr} \right) \frac{T'_{r, j+1} - 2T'_{r, j} + T'_{r, j-1}}{\Delta Y^2} + \frac{D_u \overline{C}_{r, j+1} - 2\overline{C}_{r, j} + \overline{C}_{r, j-1}}{(\Delta Y)^2} + \frac{E_c}{P_m} \left( \frac{H'_{3r, j+1} - H'_{3r, j}}{\Delta Y} \right)^2 + \frac{H'_{3r, j+1} - H'_{3r, j}}{\Delta Y} \quad (5.6)
\]
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\[
\frac{C_{T,J} - C_{T,J-1}}{\Delta \tau} + U_{T,J} \frac{C_{T,J} - C_{T-1,J}}{\Delta X} + V_{T,J} \frac{C_{T,J+1} - C_{T,J}}{\Delta Y} = \frac{1}{Sc} \frac{C_{T,J+1} - 2C_{T,J} + C_{T,J-1}}{(\Delta Y)^2} + \frac{Sr}{(\Delta Y)^2} \frac{T_{T,J+1} - 2T_{T,J} + T_{T,J-1}}{(\Delta Y)^2} - \gamma (C_{T,J})^{q'},
\]

(5.7)

with the boundary conditions

\[
U_{T,0}^{n} = 1, \quad W_{T,0}^{n} = 0, \quad H_{T,0}^{n} = 1, \quad \bar{T}_{T,0} = 1, \quad \bar{C}_{T,0} = 1,
\]

\[
U_{T,L}^{n} = 0, \quad W_{T,L}^{n} = 0, \quad H_{T,L}^{n} = 0, \quad \bar{T}_{T,L} = 0, \quad \bar{C}_{T,L} = 0 \quad \text{where} \quad L \to \infty.
\]

(5.8)

Here the subscripts \( T \) and \( J \) designate the grid points with \( X \) and \( Y \) coordinates respectively and the superscript \( n \) represents a value of time, \( \tau = n\Delta \tau \) where \( n = 0, 1, 2, \ldots \). The primary velocity \( (U) \), secondary velocity \( (W) \), primary induced magnetic field \( (H_1) \), secondary induced magnetic field \( (H_2) \), temperature \( (\bar{T}) \) and concentration \( (\bar{C}) \) distributions at all interior nodal points may be computed by successive applications of the above finite difference equations. The numerical values of the local shear stresses, local Nusselt number and local Sherwood number are evaluated by five-point approximate formula for the derivatives and then the average shear stress, current density, Nusselt number and Sherwood number are calculated by the use of Simpson’s \( \frac{1}{3} \) integration formula. The obtained values are graphically shown in Figs 3-38.

6. Results and discussion

To investigate the physical situation of the problem, the numerical values and graphs of non-dimensional primary velocity \( (U) \), secondary velocity \( (W) \), primary induced magnetic field \( (H_1) \), secondary induced magnetic field \( (H_2) \), temperature \( (\bar{T}) \) and concentration \( (\bar{C}) \) distributions within the boundary layer have been computed for different values of permeability of the porous medium \( (K) \), magnetic parameter \( (\alpha) \), magnetic parameter \( (M) \), magnetic diffusivity number \( (P_m) \), Prandtl number \( (Pr) \), Dufour number \( (Du) \), Eckert number \( (Ec) \), heat generation or absorption parameter \( (\beta) \), Schmidt number \( (Sc) \), Soret number \( (Sr) \) and chemical reaction parameter \( (\gamma) \) with the help of a computer programming language Compaq Visual Fortran 6.6a and Tecplot 7. These computed numerical results have been shown graphically. To obtain the steady-state solutions, the computation has been carried out up to \( \tau = 80 \). It is observed that the numerical values of \( U, W, H_1, H_2, \bar{T} \) and \( \bar{C} \) show little changes after \( \tau = 60 \). Hence at \( \tau = 60 \), the solutions of all variables are steady-state solutions.
To observe the physical situation of the problem, the steady-state solutions have been illustrated in Figs 3-38 when \( p = 2 \) and \( q = 2 \). The primary velocity profiles have been displayed for various values of the permeability of the porous medium \((K)\), \((\alpha)\) and magnetic parameter \((M)\) respectively illustrated in Figs 3-4a. These results show that the fluid primary velocity decreases with the increase of permeability of the porous medium. It has been observed that the primary velocity of the fluid increases within the interval \( 0 < Y < 6 \) (approx.), then decreases with the increase of \((\alpha)\). For the effects the magnetic parameter, it has been observed that the primary velocity of the fluid decreases within the interval \( 0 < Y < 6 \) (approx.) with the increase of the magnetic parameter. While reverse effects are found with the increase of the magnetic parameter. Figures 4b-5 show the secondary velocity profiles for various values of the permeability of the porous medium \((K)\), \((\alpha)\) and magnetic parameter \((M)\), respectively. It has been observed that the secondary velocity of the fluid decreases within the interval \( 0 < Y < 4 \) (approx.), then increases with the increase of permeability of the porous medium and \((\alpha)\) while opposite effects are found with the increase of the magnetic parameter. The primary induced magnetic fields have been displayed for various values of the permeability of the porous medium \((K)\), \((\alpha)\), magnetic parameter \((M)\), magnetic diffusivity number \((P_m)\) and Hall parameter \((\beta_H)\) respectively, in Figs 6-8a. These results show that the fluid primary induced magnetic field increases with the increase of the permeability of the porous medium and \((\alpha)\) while decreases with the increase of the magnetic parameter. For the effects of the magnetic diffusivity number, it has been seen that the primary induced magnetic field decreases within the interval \( 0 < Y < 16 \) (approx.), then increases for \( Y > 16 \). It has been also seen that the primary induced magnetic field increases within the interval \( 0 < Y < 11 \) (approx.), and decreases for \( Y > 16 \) with the increase of the Hall parameter. Figures 8b-10 display the secondary induced magnetic fields for various values of the permeability of the porous medium \((K)\), \((\alpha)\), magnetic parameter \((M)\), magnetic diffusivity number \((P_m)\) and Hall parameter \((\beta_H)\) respectively. These results show that the fluid secondary induced magnetic field decreases within the interval \( 0 < Y < 16 \) (approx.) with the increase of the permeability of the porous medium and \((\alpha)\) while increases for \( Y > 16 \). For the effects of the magnetic diffusivity number, the fluid secondary induced magnetic field increases within the interval \( 0 < Y < 6 \) (approx.) while opposite effects have been found for \( Y > 6 \). Figures 11-13a display the fluid temperature distributions for various values of the magnetic diffusivity number \((P_m)\), radiation parameter \((R)\), Prandtl number \((Pr)\) and heat generation or absorption parameter \((\beta)\), Dufour number \((Du)\) and Eckert number \((Ec)\), respectively. These results show that the temperature of the fluid increases with the increase of the radiation parameter, heat generation or absorption parameter, Dufour number and Eckert number, while it decreases with the increase of the Prandtl number. It is noted that \( \beta < 0 \) and \( \beta > 0 \) are treated as heat absorption and generation, respectively. As for the effects of the magnetic diffusivity number, it is observed from Fig.12a that there is no change of temperature. Figures 13b-14 show the fluid concentration for several values of the Prandtl number \((Pr)\) and heat generation or absorption parameter \((\beta)\), chemical reaction parameter \((\gamma)\) with two values of the Schmidt number \( Sc = 0.60 \) (water vapor) and \( Sc = 0.94 \) (carbon dioxide) and Soret number \((Sr)\) respectively. The concentration slightly increases within the interval \( 0 < Y < 4 \) (approx.), while opposite effects have been observed for \( Y > 4 \). But there is no change of concentration with the increase of the heat generation or absorption parameter. It is noted that the concentration decreases with the increase of the chemical reaction parameter \((\gamma)\), where \( \gamma < 0 \) and \( \gamma > 0 \) are treated as generative and destructive chemical reaction, respectively. The concentration also decreases with the increase of the Schmidt number and leads to thining of the concentration boundary layers. For the effects of the Soret
number, it has been observed that the concentration of the fluid increases with the increase of the Soret number.

Fig. 3. Illustration of primary velocity profiles for various values of (a) permeability of the porous medium \( K \) and (b) \( \alpha \) when \( p = 2 \) and \( q = 2 \).

Fig. 4. Illustration of (a) primary velocity profiles for various values of the magnetic parameter \( M \) and (b) secondary velocity profiles for various values of the permeability of the porous medium \( K \) when \( p = 2 \) and \( q = 2 \).
**Fig. 5.** Illustration of secondary velocity profiles for various values of (a) \(\alpha\) and (b) magnetic parameter \(M\) when \(p = 2\) and \(q = 2\).

**Fig. 6.** Illustration of primary induced magnetic field profiles for various values of (a) permeability of the porous medium \(K\) and (b) \(\alpha\) when \(p = 2\) and \(q = 2\).
Fig. 7. Illustration of primary induced magnetic field profiles for various values of (a) magnetic parameter \( M \) and (b) magnetic diffusivity number \( P_m \) when \( p = 2 \) and \( q = 2 \).

Fig. 8. Illustration of (a) primary induced magnetic field profiles for various values of the Hall current parameter \( \beta_e \) and (b) secondary induced magnetic field profiles for various values of the permeability of the porous medium \( K \) when \( p = 2 \) and \( q = 2 \).
Fig. 9. Illustration of secondary induced magnetic field profiles for various values of (a) \( \alpha \) and (b) magnetic parameter \( M \) when \( p = 2 \) and \( q = 2 \).

Fig. 10. Illustration of secondary magnetic induced field profiles for various values of (a) magnetic diffusivity number \( P_m \) and (b) Hall current parameter \( \beta_e \) when \( p = 2 \) and \( q = 2 \).
Fig. 11. Illustration of temperature profiles for various values of (a) magnetic diffusivity number ($P_m$) and (b) radiation parameter ($R$) when $p = 2$ and $q = 2$.

Fig. 12. Illustration of temperature profiles for various values of (a) Prandtl number (Pr) and heat generation or absorption parameter ($\beta$) and (b) Dufour number (Du) when $p = 2$ and $q = 2$. 
Fig.13. Illustration of (a) temperature profiles for various values of the Eckert number (Ec) and (b) concentration profiles for various values of the Prandtl number (Pr) and heat generation or absorption parameter ($\beta$) when $p = 2$ and $q = 2$.

Fig.14. Illustration of concentration profiles for various values of (a) Schmidt number (Sc) and chemical reaction parameter ($\gamma$) and (b) Soret number (Sr) when $p = 2$ and $q = 2$.

The average shear stresses in the $x$-direction have been shown for various values of the permeability of the porous medium ($K$), ($\alpha$) and magnetic parameter ($M$), respectively, in Figs 15-16a. These results show that the average shear stress in the $x$-direction decreases with the increase of the permeability of the porous medium and magnetic parameter while opposite effects have been observed with the increase of ($\alpha$). Figures 16b-17 show the average shear stress in the $z$-direction for various values of the permeability of the porous medium ($K$), ($\alpha$) and magnetic parameter ($M$), respectively. It has been observed that the average shear stress in the $z$-direction decreases with the increase of permeability of the porous medium and ($\alpha$) while opposite effects have occurred with the increase of the magnetic parameter. The average current densities in the $x$-direction have been displayed for various values of permeability of the porous medium.
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(K), (α), magnetic parameter (M), magnetic diffusivity number \( \left( P_m \right) \) and Hall parameter \( (\beta_e) \), respectively in Figs 18-20a. These results show that the average current density in the \( x \)-direction increases with the increase of the permeability of the porous medium, magnetic parameter and magnetic diffusivity number while opposite effects have occurred with the increase of \( (\alpha) \) and the Hall parameter. Figures 20b-22 display the average current density in the \( z \)-direction for various values of the permeability of the porous medium \( (K) \), \( (\alpha) \), magnetic parameter \( (M) \), magnetic diffusivity number \( \left( P_m \right) \) and Hall parameter \( (\beta_e) \) respectively. These results show that the average current density in the \( z \)-direction decreases with the increase of the permeability of the porous medium, magnetic parameter, magnetic diffusivity number and Hall parameter while increases with the increase of \( (\alpha) \). Figures 23-25a display the average Nusselt number for various values of the magnetic diffusivity number \( \left( P_m \right) \), radiation parameter \( (R) \), Prandtl number \( (Pr) \) and heat generation or absorption parameter \( (\beta) \), Dufour number \( (Du) \) and Eckert number \( (Ec) \), respectively. These results show that the average Nusselt number decreases with the increase of the radiation parameter, heat generation or absorption parameter, Dufour number and Eckert number, while increases with the increase of \( (\alpha) \). Figures 25b-26 show the average Sherwood number for several values of the Prandtl number \( (Pr) \) and heat generation or absorption parameter \( (\beta) \), chemical reaction parameter \( (\gamma) \) with two values of the Schmidt number \( Sc = 0.60 \) (water vapor) and \( Sc = 0.94 \) (carbon dioxide) and Soret number \( (Sr) \), respectively. The average Sherwood number decreases with the increases of the Prandtl number and increases with the increase of the heat generation or absorption parameter. It is noted that the average Sherwood number also increases with the increase of the Schmidt number. For the effects of the Soret number, it has been observed that the average Sherwood number increases with the increase of the Soret number.

Fig.15. Illustration of average shear stress in the \( x \)-direction for various values of (a) permeability of the porous medium \( (K) \) and (b) \( (\alpha) \) when \( p = 2 \) and \( q = 2 \).
Fig. 16. Illustration of (a) average shear stress in the $x$-direction for various values of the magnetic parameter ($M$) and (b) average shear stress in the $z$-direction for various values of permeability of the porous medium ($K$) when $p = 2$ and $q = 2$.

Fig. 17. Illustration of average shear stress in the $z$-direction for various values of (a) $\alpha$ and (b) magnetic parameter ($M$) when $p = 2$ and $q = 2$.
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Fig. 18. Illustration of average current density in the $x$-direction for various values of (a) permeability of the porous medium ($K$) and (b) ($\alpha$) when $p = 2$ and $q = 2$.

Fig. 19. Illustration of average current density in the $x$-direction for various values of (a) magnetic parameter ($M$) and (b) magnetic diffusivity number ($P_m$) when $p = 2$ and $q = 2$. 
Fig. 20. Illustration of (a) average current density in the $x$-direction for various values of the Hall current parameter ($\beta_e$) and (b) average current density in the $z$-direction for various values of the permeability of the porous medium ($K$) when $p = 2$ and $q = 2$.

Fig. 21. Illustration of average current density in the $z$-direction for various values of (a) ($\alpha$) and (b) magnetic parameter ($M$) when $p = 2$ and $q = 2$. 
Fig. 22. Illustration of average current density in the $z$-direction for various values of (a) magnetic diffusivity number ($P_m$) and (b) Hall current parameter ($\beta_e$) when $p = 2$ and $q = 2$.

Fig. 23. Illustration of average Nusselt number for various values of (a) magnetic diffusivity number ($P_m$) and (b) radiation parameter ($R$) when $p = 2$ and $q = 2$. 
Fig. 24. Illustration of average Nusselt number for various values of (a) Prandtl number (Pr) and heat generation or absorption parameter (β) and (b) Dufour number (Du) when $p = 2$ and $q = 2$.

Fig. 25. Illustration of (a) average Nusselt number for various values of the Eckert number (Ec) and (b) average Sherwood number for various values of the Prandtl number (Pr) and heat generation or absorption parameter (β) when $p = 2$ and $q = 2$. 
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Fig. 26. Illustration of average Sherwood number for various values of (a) Schmidt number (Sc) and chemical reaction parameter $\gamma$ (b) Soret number (Sr) when $p = 2$ and $q = 2$.

The local shear stresses in the $x$-direction have been shown for various values of the permeability of the porous medium ($K$), ($\alpha$) and magnetic parameter ($M$), respectively, in Figs 27-28a. These results show that the local shear stress in the $x$-direction decreases with the increase of the permeability of the porous medium and magnetic parameter while opposite effects have occurred with the increase of ($\alpha$). Figures 28b-29 show the local shear stress in the $z$-direction for various values of the permeability of the porous medium ($K$), ($\alpha$) and magnetic parameter ($M$), respectively. It has been observed that the local shear stress in the $z$-direction decreases with the increase of permeability of the porous medium and ($\alpha$) while opposite effects have been observed with the increase of the magnetic parameter. The local current densities in the $x$-direction have been illustrated for various values of the permeability of the porous medium ($K$), ($\alpha$), magnetic parameter ($M$), magnetic diffusivity number ($P_m$) and Hall parameter ($\beta_e$) respectively, in Figs 30-32a. These results show that the local current density in the $x$-direction increases with the increase of the permeability of the porous medium, magnetic parameter and magnetic diffusivity number while opposite effects have been observed with the increase of ($\alpha$) and Hall parameter. Figures 32b-34 display the local current density in the $z$-direction for various values of the permeability of the porous medium ($K$), ($\alpha$), magnetic parameter ($M$), magnetic diffusivity number ($P_m$) and Hall parameter ($\beta_e$) respectively. These results show that the local current density in the $z$-direction decreases with the increase of the permeability of the porous medium, magnetic parameter, magnetic diffusivity number and Hall parameter while opposite effects have been observed with the increase of ($\alpha$).

Figures 35-37a display the local Nusselt number for various values of the magnetic diffusivity number ($P_m$), radiation parameter ($R$), Prandtl number (Pr) and heat generation or absorption parameter ($\beta$), Dufour number (Du) and Eckert number (Ec), respectively. These results show that the local Nusselt number decreases with the increase of the heat generation or absorption parameter, Dufour number and Eckert number while increases with the increase of the Prandtl number, where $\beta < 0$ and $\beta > 0$ are treated as heat absorption and generation, respectively. As for the effects of the magnetic diffusivity number and radiation parameter, it is observed from Fig.35 that there is no change of the local Nusselt number.
Figures 37b-39 display the local Sherwood number for several values of the Prandtl number (Pr) and heat generation or absorption parameter ($\beta$), chemical reaction parameter ($\gamma$) with two values of Schmidt number Sc = 0.60 (water vapor) and Sc = 0.94 (carbon dioxide) and Soret number (Sr), respectively. The local Sherwood number decreases with the increases of the Prandtl number while there is no change with the increase of the heat generation or absorption parameter. It is noted that the local Sherwood number increases with the increase of the chemical reaction parameter ($\gamma$), where $\gamma < 0$ and $\gamma > 0$ are treated as generative and destructive chemical reaction, respectively. The local Sherwood number also increases with the increase of the Schmidt number. For the effects of the Soret number, it has been observed that the local Sherwood number decreases with the increase of Soret number.

Fig.27. Illustration of local shear stress in the $x$-direction for various values of (a) permeability of the porous medium ($K$) and (b) ($\alpha$) when $p = 2$ and $q = 2$.

Fig.28. Illustration of (a) local shear stress in the $x$-direction for various values of the magnetic parameter ($M$) and (b) local shear stress in the $z$-direction for various values of the permeability of the porous medium ($K$) when $p = 2$ and $q = 2$. 
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Fig. 29. Illustration of local shear stress in the $z$-direction for various values of (a) $(\alpha)$ and (b) magnetic parameter $(M)$ when $p = 2$ and $q = 2$.

Fig. 30. Illustration of local current density in the $x$-direction for various values of (a) permeability of the porous medium $(K)$ and (b) $(\alpha)$ when $p = 2$ and $q = 2$. 
Fig. 31. Illustration of local current density in the $x$-direction for various values of (a) magnetic parameter ($M$) and (b) magnetic diffusivity number ($P_m$) when $p = 2$ and $q = 2$.

Fig. 32. Illustration of (a) local current density in the $x$-direction for various values of the Hall current parameter ($\beta_c$) and (b) local current density in the $x$-direction for various values of the permeability of the porous medium ($K$) when $p = 2$ and $q = 2$. 
Fig. 33. Illustration of average current density in the \( z \)-direction for various values of (a) \( \alpha \) and (b) magnetic parameter \( M \) when \( p = 2 \) and \( q = 2 \).

Fig. 34. Illustration of local current density in the \( z \)-direction for various values of (a) magnetic diffusivity number \( P_m \) and (b) Hall current parameter \( \beta_e \) when \( p = 2 \) and \( q = 2 \).
Fig. 35. Illustration of the local Nusselt number for various values of (a) magnetic diffusivity number \( P_m \) and (b) radiation parameter \( R \) when \( p = 2 \) and \( q = 2 \).

Fig. 36. Illustration of local Nusselt number for various values of (a) Prandtl number (Pr) and heat generation or absorption parameter \( \beta \) and (b) Dufour number (Du) when \( p = 2 \) and \( q = 2 \).
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7. Conclusions

The explicit finite difference solution for considerable magnetic Reynolds number of unsteady chemically reacting radiative ionized fluid flow over an impulsive vertical porous plate in the presence of heat generation, and Joule heating for \( p \leq 2 \) and \( q \leq 2 \) has been investigated. The physical properties are graphically discussed for different values of corresponding parameters and our steady-state results are compared with Haque et al. [12]. The accuracy of our results is qualitatively good in for all the flow parameters.

Some important findings of this investigation are listed below;
1. The average and local shear stress in the \( x \)-direction decreases with the increase of the permeability of
the porous medium and magnetic parameter, while it increases with the increase of \((\alpha)\).

2. The average and local shear stress in the \(z\)-direction decreases with the increase of the permeability of the porous medium and \((\alpha)\) whereas it increases with the increase of the magnetic parameter.

3. The average and local current density in the \(x\)-direction increases with the increase of the permeability of the porous medium, magnetic parameter and magnetic diffusivity number, while it decreases with the increase of \((\alpha)\) and Hall parameter.

4. The average and local current density in the \(z\)-direction decreases with the increase of the permeability of the porous medium, magnetic parameter, magnetic diffusivity number and Hall parameter, while it decreases with the increase of \((\alpha)\).

5. The average and local Nusselt number decreases with the increase of the Dufour number, heat generation or absorption parameter and Eckert number whereas reverse effects have been observed with the increase of the Prandtl number.

6. The average and local Sherwood number decreases with the increase of the Prandtl number and Soret number while reverse effects have been found with the increase of the heat generation or absorption parameter, Schmidt number and chemical reaction parameter.

The findings of this investigation may be useful for the study of movement oil or gas and water through the reservoirs of an oil or gas field, in the migration of underground water or oil as well as in the filtration and water purification processes. These results may also be useful for plasma studies as well as in power engineering, geothermal energy extraction, geophysics and astrophysics.

Nomenclature

- \(C\) – species concentration
- \(\bar{C}\) – dimensionless concentration
- \(c_p\) – specific heat at the constant pressure
- \(c_s\) – concentration susceptibility
- \(D\) – coefficient of mass diffusivity
- \(\text{Du}\) – Dufour number
- \(\text{Er}\) – Eckert number
- \(\text{Gm}\) – modified Grashof Number
- \(\text{Gr}\) – Grashof Number
- \(g\) – local acceleration due to gravity
- \(\mathbf{H}\) – resultant magnetic field vector
- \(H_0\) – imposed uniform magnetic field
- \(H_1\) and \(H_2\) – dimensionless primary and secondary induced magnetic field
- \(H_x, H_y\) and \(H_z\) – components of magnetic induction vector in the three directions
- \(H_w\) – magnetic induction at the wall
- \(\mathbf{J}\) – current density vector
- \(J_x, J_y\) and \(J_z\) – current densities in the three directions
- \(j_{xL}\) – local current density in the \(x\)-direction
- \(j_{xA}\) – average current density in the \(x\)-direction
- \(j_{zL}\) – local current density in the \(z\)-direction
- \(j_{zA}\) – average current density in the \(z\)-direction
- \(K\) – permeability of the porous medium
- \(k^*\) – mean absorption coefficient
- \(k_0\) – rate of chemical reaction
- \(k_t\) – thermal diffusion ratio
- \(M\) – magnetic parameter
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- \( \text{Nu}_L \) – local Nusselt number
- \( \text{Nu}_A \) – average Nusselt number
- \( P_m \) – magnetic diffusivity number
- \( \text{Pr} \) – Prandtl number
- \( p, q \) – positive constants
- \( R \) – radiation parameter
- \( q_r \) – radiative heat flux
- \( \text{Sc} \) – Schmidt number
- \( \text{Sh}_L \) – local Sherwood number
- \( \text{Sh}_A \) – average Sherwood number
- \( \text{Sr} \) – Soret number
- \( T \) – temperature
- \( \mathcal{T} \) – dimensionless temperature
- \( T_w, C_w \) – temperature and species concentration at the wall
- \( T_\infty, C_\infty \) – temperature and concentration of the species outside the plate
- \( t \) – time
- \( U, V \) and \( W \) – dimensionless velocity components in three directions
- \( U_\infty \) – constant velocity of plate movement
- \( u, v \) and \( w \) – velocities in the three directions
- \( v_0 \) – suction velocity
- \( X_{\text{max}} \) – maximum length of the plate
- \( x, y \) and \( z \) – Cartesians co-ordinates in the three directions
- \( Y \) – dimensionless Cartesian coordinate in the \( y \)-direction
- \( Y_{\text{max}} \) – maximum length of the boundary layer
- \( \alpha \) – uniform magnetic field \( H_0 \) applied in a direction that makes an angle with the normal to the considered plate
- \( \beta \) – heat generation or absorption parameter
- \( \beta_C \) – concentration expansion coefficient
- \( \beta_T \) – thermal expansion coefficient
- \( \gamma \) – chemical reaction parameter
- \( \kappa \) – thermal conductivity
- \( \mu \) – fluid viscosity
- \( \mu_e \) – magnetic permeability
- \( \rho \) – density of the fluid
- \( \sigma^* \) – the Stefan-Boltzman constant
- \( \tau \) – dimensionless time
- \( \tau_{xL} \) – local shear stress in the \( x \)-direction
- \( \tau_{xA} \) – average shear stress in the \( x \)-direction
- \( \tau_{zL} \) – local shear stress in the \( z \)-direction
- \( \tau_{zA} \) – average shear stress in the \( z \)-direction
- \( \nu \) – kinematic coefficient viscosity

References


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