# LATVIAN JOURNAL OF PHYSICS AND TECHNICAL SCIENCES <br> 2017, N 2 

DOI: 10.1515/lpts-2017-0013

# THEORETICAL ANALYSIS OF SPACING PARAMETERS OF ANISOTROPIC 3D SURFACE ROUGHNESS 

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#### Abstract

The authors of the research have analysed spacing parameters of anisotropic 3D surface roughness crosswise to machining (friction) traces $R S m$, and lengthwise to machining (friction) traces $R S m_{2}$. The main issue arises from the $R S m$, values being limited by values of sampling length $l$ in the measuring devices; however, on many occasions $R S m_{2}$ values can exceed $l$ values. Therefore, the mean spacing values of profile irregularities in the longitudinal direction in many cases are not reliable and they should be determined by another method. Theoretically, it is proved that anisotropic surface roughness anisotropy coefficient $c=R S m_{l} / R S m_{2}$ equals texture aspect ratio $S t r$, which is determined by surface texture standard EN ISO 25178-2. This allows using parameter Str to determine mean spacing of profile irregularities and estimate roughness anisotropy.


Keywords: anisotropy coefficient, roughness spacing parameters, surface texture, texture aspect ratio.

## 1. INTRODUCTION

As a result of introducing surface texture standard (EN ISO 25178-2) [1], interest in 3D surface roughness parameters is growing. Knowing spacing parameters of the 3D surface roughness, especially if surface roughness is anisotropic, is an important factor in solving different technical tasks (friction, wear, part contacting etc.).

Surface roughness is anisotropic if in different surface directions profiles are different, unlike isotropic surface roughness that has the same profiles in all directions.

The main interest lies in surfaces with anisotropy in mutually perpendicular directions. In such a case, roughness mean spacing of profile irregularities is as follows: $R S m_{1}$ - crosswise to machining (friction) traces and $R S m_{2}$ - lengthwise to machining (friction) traces (Fig. 1).


Fig. 1. Example of 3D surface with anisotropic roughness.

Engineering tasks require that the spacing parameters be easily identifiable and technologically feasible in machining. Otherwise, these parameters have no practical value.

In standard EN ISO 4287 [2], spacing parameter $R S m$ is defined as mean width of profile elements along the mean line of the profile.

However, the ratio between spacing parameters $R S m_{1}$ and $R S m_{2}$, which characterises the anisotropy of surface roughness, is not defined in standards. Yet it is an important value that is required for characterising surface anisotropy and is used by surface scientists [5]-[10].

Based on the uniformed surface characterisation, the control bases of these parameters - mean lines - should be located at the level of the mean plane of rough surface (Fig. 2). Then these spacing parameters characterise a 3D surface.


Fig. 2. Placement scheme of 3D surface roughness spacing parameters.

The authors of the paper have designated the ratio between spacing parameters as $c$ :

$$
\begin{equation*}
c=\frac{R S m_{1}}{R S m_{2}} \tag{1}
\end{equation*}
$$

Parameter $c$ is identified as an anisotropy coefficient. If surface is isotropic, $R S m_{1}=R S m_{2}$ and $c=1$. However, if surface is anisotropic, $R S m_{2} \rightarrow \infty, c \rightarrow 0$.

Current 3D surface roughness measurement devices, for instance, Taylor Hobson Intra 50, identify the spacing parameters without linking the mean line of the profile with the mean plane of the surface. This results in significantly lower RSm
values and notably influences parameter $R S m_{2}$. This can be clearly seen in Fig. 3, which shows values of parameters $S a, R S m_{1}$ and $R S m_{2}$ of a grinded surface with irregular surface roughness ( $S a$ - arithmetic mean height of the scale limited surface). Surface roughness measurements that are used in this paper hereinafter were obtained using Taylor Hobson measuring equipment Intra 50.


Fig. 3. Parameter values of grinded surface.

3D surface roughness parameter for the grinded surface shown in Fig. 3 is $S a=0.048 \mu \mathrm{~m}$, and this parameter is identified as a deviation from the roughness mean plane. If the mean plane is also crossed by roughness sections (profiles), profile arithmetic mean deviation value $R a$ should be close to the 3D surface value $S a$ (in theory, at infinite number of profiles $R a \rightarrow S a)$.

In the given example (Fig. 3), surface roughness in crosswise direction is $R a_{1}=0.038 \mu \mathrm{~m}$, which is close to $S a=0.048 \mu \mathrm{~m}$. Thus, it can be assumed that the mean line of crosswise profile of surface roughness is closely positioned to surface roughness mean plane. Thus, the mean spacing of profile irregularities $R S m_{l}$ can be assumed as a value of the crosswise mean spacing of profile irregularities belonging to the 3D surface roughness, and in this case $R S m_{l}=0.088 \mathrm{~mm}$. It can be clearly seen from the form of the crosswise profile (Fig. 3). The profile in question has 9 visible irregularities (Fig. 3, marked with a tick) along the evaluation length $L=0.8 \mathrm{~mm}$ enabling one to approximately estimate that $R S m_{1} \approx L / 9=0.8 / 9=0.089 \mathrm{~mm}$. This value is close to the value determined by the measuring equipment, i.e., $R S m_{l}=0.088 \mathrm{~mm}$. Hereinafter, such a way of determining spacing parameters will be called the visual determination method.

This method will also be used for other surface profiles that are given reduced values of mean spacing of profile irregularities by the measuring equipment comparing to the real values.

The example (Fig. 3) shows a slightly different situation regarding surface roughness in longitudinal direction, with $R a_{2}=0.006 \mu \mathrm{~m}$ substantially differing from $S a=0.048 \mu \mathrm{~m}$. This shows that the mean line of the longitudinal profile of surface roughness is distant from the mean plane of surface roughness, and the mean value of the mean spacing of profile irregularities is $R S m_{2}=0.130 \mathrm{~mm}$, which is not accurate and does not characterise surface anisotropy correctly. This value cannot be used in formula (1) to determine anisotropy coefficient $c$. The visual method, in turn,
allows one to determine $\mathrm{RSm}_{2}$ value more accurately. The profile in question has approximately 2 irregularities along the evaluation length $L=0.8 \mathrm{~mm}$. Consequently, $R S m_{2} \approx L / 2=0.8 / 2=0.4 \mathrm{~mm}$, which is approximately 3 times the value determined by the measuring equipment, i.e., $R S m_{2}=0.130 \mathrm{~mm}$. It can be seen with unaided eye that this value is more probable (Fig. 3).

It can be concluded that there is a big difference in the results depending on whether the values of mean spacing of profile irregularities $R S m_{2}$ (surface in Fig. 3) were measured with measuring equipment or using the visual determination method.

How to determine the value of 3D surface parameter $R \mathrm{Rm}_{2}$ ? Apparently, one can use parameter Str - a texture aspect ratio provided in standard EN ISO 25178-2.

## 2. TEXTURE ASPECT RATIO

According to American National Standard ASME B46.1-2009 "Surface Texture" [4] and [3]:

$$
\begin{equation*}
S t r=\frac{L_{F}}{L_{s l}} \tag{2}
\end{equation*}
$$

where $L_{F}$ - length of the fastest decay of ACF;
$L_{S l}$ - length of the slowest decay of ACF;
ACF - the autocorrelation function.

Mathematical expression of ACF between two points with coordinates ( $\mathrm{x}_{1} ; \mathrm{y}_{1}$ ) and $\left(\mathrm{x}_{2} ; \mathrm{y}_{2}\right)$ can be written as $\rho\left(\tau_{1} ; \tau_{2}\right)$, where $\tau_{1}^{\prime}=x_{2-} x_{1}$ distance between points on axis $x$ and $\tau_{2}=y_{2} y_{1}$ - distance between points on axis $y$. When the distance between the points increases (by increase of values $\tau_{1}$ and $\tau_{2}$ ), values $\rho\left(\tau_{1} ; \tau_{2}\right)$ decrease (Fig. 4).


Fig. 4. Schematic representation of surface roughness (a) and corresponding standardised correlation function (b) [7].

Decrease rate of values of the correlation function can be characterised by correlation interval $\tau \mathrm{k}$, which for the particular section is determined as follows:

$$
\begin{equation*}
\tau_{k}=\int_{0}^{\infty}|\rho(\tau)| d t \tag{3}
\end{equation*}
$$

where $\rho(\tau)$ - the autocorrelation function of surface roughness section.

Geometrically, $\tau_{k}$ is length of an edge of a rectangular base, the other edge of which is 1 and the area is equal to an area of a standardized correlation function under the curve. Value of $\tau_{k}$ for surface depends on the properties of the section.

In case of anisotropic surface roughness, the surface correlation function can be placed differently towards axes x , y (Fig. 5).


Fig. 5. Schematic placement of $\tau_{\mathrm{k}}$ [1]
$a$ - the correlation function is oriented along axes $x$ and $y, b-$ the correlation function is not oriented along axes x and y .

Assuming that the correlation function $\rho\left(\tau_{l} ; \tau_{2}\right)$ is oriented along base-directions of anisotropic rough surface: $\tau_{1}$ axis along direction $\mathrm{x}, \tau_{2}$ axis along direction y . This means that $L_{F}=\tau_{k \min }=\tau_{k x}$, but $L_{S l}=\tau_{k \max }=\tau_{k y}$ because the surface profile has greater irregularity density crosswise to machining (friction) traces and the correlation function is descending faster as well. Thus, according to formula (2), it can be represented as follows:

$$
\begin{equation*}
\text { Str }=\frac{\tau_{k x}}{\tau_{k y}} \tag{4}
\end{equation*}
$$

It should be noted that standard EN ISO 25178-2 [1] foresees that the autocorrelation function is determined at level $0 \leq s \leq 1$ (usually $s=0.2$ ). However, at any level of $s$, ratio (4) retains its basic value; therefore, formula (4) can be used to characterise parameter Str at any $s$ value, without losing the general approach.

Using studies on correlation functions of profiles of irregular rough surfaces [7], for a monotonically decreasing function:

$$
\begin{equation*}
\tau_{k}=\frac{\tau_{k n}}{E\{n(0)\}}, \tag{5}
\end{equation*}
$$

where $\tau_{k n}$ - the standardised value of the correlation interval. It is constant for the particular correlation function.
$E\{n(0)\}$ - mathematical expectation of intersections with the mean line of the roughness profile (zero count).

In accordance with formula (4) for the particular correlation function:

$$
\begin{equation*}
\operatorname{Str}=\frac{E\left\{n_{2}(0)\right\}}{E\left\{n_{1}(0)\right\}}, \tag{6}
\end{equation*}
$$

where indices 1 and 2 characterise crosswise and longitudinal profiles, respectively. Since $E\{n(0)\}=2 / R S m[7]$, then:

$$
\begin{equation*}
S t r=\frac{R S m_{1}}{R S m 2} . \tag{7}
\end{equation*}
$$

Comparing the obtained formula (7) with (1), one gets important data for determining surface anisotropy coefficient $c$ :

$$
\begin{equation*}
S t r=c . \tag{8}
\end{equation*}
$$

This means that the correlation function, which is orientated along the surface directions, allows using parameter Str to determine anisotropic coefficient $c$.

## 3. $R S M_{2}$ DETERMINATION

Using oriented correlation function of surface roughness in accordance with formula (8), $R \mathrm{Rm}_{2}$ value can be easily determined:

$$
\begin{equation*}
R S m_{2}=\frac{R S m_{1}}{S t r}, \tag{9}
\end{equation*}
$$

where parameter $\operatorname{Str}$ is determined with the corresponding measuring equipment, such as Taylor Hobson Intra 50.

In general situations, when there are no notable mutually perpendicular basedirections of surface roughness, formulas (7), (8), (9) cannot be applied, for instance, for a cylinder liner of an internal combustion engine machined by honing operation.

There is another way to determine $R \mathrm{Rm}_{2}$.
Random field theory, which allows connecting 3D surface parameters with engineering tasks (surface contact, friction, wear etc.), is becoming increasingly popular in the modelling of irregular surface roughness (abrasion, worn surfaces etc.) [6], [7], [8].

If surface roughness is described with a random field, using theory of normal random field [10]:

$$
\begin{equation*}
E^{2}\left\{n_{\phi}(0)\right\}+E^{2}\left\{n_{\phi+90^{\circ}}(0)\right\}=\text { const } \text {, } \tag{10}
\end{equation*}
$$

where $n_{\varphi}(0)$ - the number of zeroes of section at angle $\varphi$ of normal random field (number of intersections between the profile and mean line);
$n_{\varphi+90^{\circ}}(0)$ - the number of zeroes of section at angle $\varphi+90^{\circ}$ of normal random field;
$\mathrm{E}\}$ - mathematical expectation of random variable.

According to the given formula, sum of squares of zeroes of any 2 mutually perpendicular sections is constant. Consequently, it can be written as follows:

$$
\begin{equation*}
E^{2}\left\{n_{0^{\circ}}(0)\right\}+E^{2}\left\{n_{90^{\circ}}(0)\right\}=E^{2}\left\{n_{45^{\circ}}(0)\right\}+E^{2}\left\{n_{135^{\circ}}(0)\right\} . \tag{11}
\end{equation*}
$$

Assuming that section at $\varphi=0^{\circ}$ is the first direction (in the direction of axis x ) and $\varphi=90^{\circ}$ is the second direction (in the direction of axis y), formula (11) can be simplified:

$$
\begin{equation*}
E^{2}\left\{n_{1}(0)\right\}+E^{2}\left\{n_{2}(0)\right\}=E^{2}\left\{n_{45^{\circ}}(0)\right\}+E^{2}\left\{n_{135^{\circ}}(0)\right\} . \tag{12}
\end{equation*}
$$

If the profiles are taken at $\varphi=45^{\circ}$ and $135^{\circ}$, the number of zeroes is the same:

$$
\begin{equation*}
E^{2}\left\{n_{45^{\circ}}(0)\right\}=E^{2}\left\{n_{135^{\circ}}(0)\right\} . \tag{13}
\end{equation*}
$$

From expressions (12), (13) it can be concluded that:

$$
\begin{equation*}
E^{2}\left\{n_{2}(0)\right\}=2 \cdot E^{2}\left\{n_{45^{\circ}}(0)\right\}-E^{2}\left\{n_{1}(0)\right\} . \tag{14}
\end{equation*}
$$

Dividing both sides by $E^{2}\left\{n_{1}(0)\right\}$, one gets:

$$
\begin{equation*}
c^{2}=2 \cdot\left[\frac{E\left\{n_{45^{\circ}}(0)\right\}}{E\left\{n_{1}(0)\right\}}\right]^{2}-1, \tag{15}
\end{equation*}
$$

where $c$ - the anisotropy coefficient (see (1)).

$$
\begin{equation*}
c=\frac{E\left\{n_{2}(0)\right\}}{E\left\{n_{1}(0)\right\}}=\frac{E\left\{R S m_{1}\right\}}{E\left\{R S m_{2}\right\}} . \tag{16}
\end{equation*}
$$

Using formula (1),

$$
\begin{equation*}
R S m_{2}=\frac{R S m_{1}}{c} \tag{17}
\end{equation*}
$$

It should be noted that this approach has two disadvantages:

1) a need for additional information to determine $n_{45^{\circ}}(0)$;
2) the method is limited by expression (15) that determines the following:

$$
\begin{equation*}
\frac{\sqrt{2}}{2} \leq \frac{E\left\{n_{45^{5}}(0)\right\}}{E\left\{n_{1}(0)\right\}} \leq 1.0 . \tag{18}
\end{equation*}
$$

If the experimental values $\mathrm{n}_{1}(0)$ and $\mathrm{n}_{45^{\circ}}(0)$ do not result in formula (18), parameter $R \mathrm{Sm}_{2}$ should be obtained applying the visual method (see paragraph 1).

It should be taken into account that the suggested $R \mathrm{Rm}_{2}$ determination method significantly differs from the classical surface roughness metrology if surface roughness is anisotropic. In compliance with the classical metrology, all surface roughness parameters are determined within the limits of sampling length $l$ [2]. However, in the given approach, using formulas (9) and (17), $R S m_{2}$, values can even exceed sampling length $l$, which is selected according to the value of parameter $R a$ (see Table 2).

In classical metrology, such $R S m_{2}$ values could be viewed as waviness mean spacing; however, mean spacing of profile elements $R S m_{1}$ and $R S m_{2}$ essentially characterise one but very longitudinally stretched irregularity, which has formed due to friction, wear, grinding or any other similar process. Physically, it is not linked to waviness.

Consequently, this $R S m_{2}$ value should be used in friction-, wear- and other technical calculations where mean spacing of profile elements for surface roughness has to be taken into account.

## 4. CONCLUSIONS

Within the framework of the research, the authors have evaluated anisotropy of surface roughness. First of all, the mean spacing values of profile irregularities obtained by measuring equipment have been analysed for flat grinded surface. It has been stated that mean spacing values of profile irregularities in longitudinal direction are not reliable due to the fact that surface mean plane and profile mean line are located at different levels. In addition, for the initial determination of roughness of mean spacing of profile irregularities $R S m_{2}$ the visual method has been proposed. Secondly, anisotropy coefficient $c$ and surface texture aspect ratio $S t r$ have been compared. During the theoretical study, it has been substantiated by formulas that surface texture parameter Str, which is standardised in ISO 25178-2:2012, can be used to evaluate roughness anisotropy and calculate spacing parameters.

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# ANIZOTROPĀ 3D VIRSMAS RAUPJUMA SOL̦A PARAMETRU TEORĒTISKĀ ANALĪZE 

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## Kopsavilkums

Dotajā zinātniskajā darbā veikta anizotropiska 3D virsmas raupjuma soḷa parametru analīze, šķērsām apstrādes (berzes) pēdām $R S m_{l}$ un paralēli apstrādes (berzes) pēdām $R S m_{2}$. Problēmas būtība ir tā, ka $R S m_{2}$ vērtības mēraparātos ir ierobežotas ar bāzes garuma $l$ vērtībām, kaut gan vairākos gadījumos virsmas $R \mathrm{Sm}_{2}$ vērtības var pārsniegt $l$ vērtības. Tāpēc arī soḷa parametra vērtības garenvirzienā vairākos gadījumos nav ticamas un tās ir jānosaka ar citu paņēmienu. Teorētiski ir pierādīts, ka anizotropa virsmas raupjuma gadījumā anizotropijas koeficients $c=R S m_{1} / R S m_{2}$ ir vienāds ar virsmas tekstūras indeksu Str, kuru nosaka virsmas tekstūras standarts EN ISO 25178-2. Sakarā ar to, parametru Str ir iespēja pielietot raupjuma soḷu noteikšanai un raupjuma anizotropijas novērtēšanai.
12.07.2016.

