

## VISIBILITY AND GEOMETRY OF GLOBAL SATELLITE NAVIGATION SYSTEMS CONSTELLATIONS

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**ABSTRACT.** Nowadays (November 2015) there are two global fully operational satellite navigation systems, American GPS and Russian GLONASS. Two next are under construction, Galileo in Europe and BeiDou in China. As the error of observer's position obtained from these systems depends on geometry factor DOP (Dilution Of Precision) among other things the knowledge of the number of satellites visible by this observer above given masking elevation angle  $H_{\min}$  and the distributions of DOP coefficient values, GDOP in particular, is very important. The lowest and the greatest number of satellites visible in open area by the observer at different latitudes for different  $H_{\min}$ , the percentage of satellites visible above angle  $H$  (9 intervals, each  $10^\circ$  wide), distributions (in per cent) of satellites azimuths (8 intervals, each  $45^\circ$  wide) and GDOP coefficient values (8 intervals) for  $H_{\min} = 5^\circ$  for all these four systems at different observer's latitudes (9 intervals, each wide  $10^\circ$  wide) are presented in the paper. Additionally the lowest elevation for which the number of satellites visible at different latitudes by the observer in open area above this angle is equal 4 or 3 and the distributions (in per cent) of GDOP coefficient values for different  $H_{\min}$  at observer's latitudes  $50\text{--}60^\circ$  for the same four systems are showed. All calculations were made for constellation of GPS 27 satellites, GLONASS 24, Galileo 30 and BeiDou 27 MEO satellites.

**Keywords:** GPS constellation, GLONASS constellation, Galileo constellation, BeiDou constellation, visibility, geometry

### 1. INTRODUCTION

The error  $M$  of the observer's position obtained from satellite navigation system depends on geometry factor DOP (Dilution of Precision) among other things. That's why the knowledge of the number of satellites visible at given moment by this observer above given masking elevation angle  $H_{\min}$  and the distributions of DOP, GDOP in particular, coefficient value is very important (Hofmann–Wellenhof B. et al 2008), (Kaplan E.D., Hegarty C.J. 2006), (Langley R.B. 1999), (Specht C. 2007).

Nowadays (August 2015) there are two global fully operational satellite navigation systems (SNS), American GPS and Russian GLONASS (Martin III H.W. 2015), (Karutin S 2015), ([www.glonass-ianc.rsa.ru](http://www.glonass-ianc.rsa.ru)), ([www.gps.gov](http://www.gps.gov)), ([www.gpsworld.com](http://www.gpsworld.com)), ([navcen.uscg.gov](http://navcen.uscg.gov)). Two next SNS are under construction, Galileo in Europe and BeiDou in China (Chatre E, 2015), (China Satellite Navigation Summit, 2015), ([www.esa.int](http://www.esa.int)).

Global services Galileo and BeiDou will both provide by around 2017/2018 or later ([www.beidou.gov.cn](http://www.beidou.gov.cn)), ([www.insidegnss.com](http://www.insidegnss.com)). The final BeiDou space constellation will consist of 35 satellites (27 MEO, 5 GEO, 3 IGSO) but as the signals transmitted by all GEO and IGSO satellites can be used in some regions of the Earth (China and adjacent areas) merely, the 27 MEO satellites were taken into account only (Munich 2015). In order to compare BeiDou MEO and GPS (MEO also) constellations it was assumed that the number American system satellites is equal 27 too even though since several years this number is incessantly at least 29 or 30 ([www.gps.gov](http://www.gps.gov)), ([www.gpsworld.com](http://www.gpsworld.com)). In the case of GLONASS and Galileo the number of satellites is equal 24 (actual nominal constellation) and 30 (final constellation with 3 planes and 9 operational satellites and one active spare per orbital plane), respectively ([www.glonass-ianc.rsa.ru](http://www.glonass-ianc.rsa.ru)), ([www.insidegnss.com](http://www.insidegnss.com)). All 24 GLONASS, all 27 MEO BeiDou and all 27 operational Galileo satellites were evenly distributed on the orbits.

The parameters of the spatial segment and coverage surface area ensured by one satellite only of all four mentioned above SNSs are presented in Table 1 (Januszewski J, 2010), ([www.gps.gov](http://www.gps.gov)), ([www.insidegnss.com](http://www.insidegnss.com)). In calculations it was assumed the radius of the Earth 6,370 km and the Earth's surface 510,066,000 km<sup>2</sup>. Because Galileo orbit altitude is the highest the coverage surface area is in the case of this system the greatest, near 40 % of the Earth.

**Table 1.** Spatial segment and coverage surface area of GPS, GLONASS, Galileo and BeiDou systems

System	Number of MEO orbits	Number of satellites		Orbit altitude [km]	Orbital period	Coverage surface area (one satellite only)	
		on one orbit	total			[ km <sup>2</sup> ]	% of the Earth
GPS	6	4 ÷ 6	27	20,183	11 h 57 min 58.3 sec	193 705 518	38.0
GLONASS	3	8	24	19,100	11 h 15 min 44 sec	191 117 254	37.5
Galileo	3	10	30	23,222	14 h 4 min 45 sec	199 969 523	39.2
BeiDou	3	9	27	21,500	12 h 56 min 16.05 sec	196 773 430	38.6

## 2. TEST METHOD

All calculations based on reference ellipsoid WGS-84 were made on author's simulating program. The interval of the latitude of the observer between 0° and 90° was divided into 9 zones, each 10° wide. In the observer's receiver masking elevation angle  $H_{\min}$  was assumed to be 0° (horizon), 5° (the most frequently used value of  $H_{\min}$ ), 10°, 15°, 20° and 25°. The angle 25° is representative for the positioning in restricted area where the visibility of satellites can be limited. This problem is very important in road transport (urban canyon) and in maritime transport. As the GLONASS, Galileo and BeiDou satellites are evenly distributed amongst orbital planes and for all four SNSs appropriate time interval was taken into account in calculation the analyses concern both hemispheres.

For each system, for each zone of latitude and for each angle ( $H_{\min}$ ) one thousand (1000) geographic time coordinates of the observer were generated by random-number generator with uniform distribution:

- latitude interval 0 – 600 min (10°),
- longitude interval 0 – 21600 min (360°),
- time interval (in minutes): 0 – 1,435.94 (GPS, 2 orbital periods), 0 – 11,488.44 (GLONASS, 17 orbital periods), 0 – 14,360.75 (Galileo, 17 orbital periods), 0 – 10,091.48 (BeiDou, 13 orbital periods).

For each geographic–time coordinates: the satellite elevation ( $H$ ), the satellite azimuth ( $Az$ ), the number of visible satellites ( $Is$ ) and GDOP (Geometric Dilution of Precision) coefficient values were calculated. Elevation  $H$  was divided into 9 intervals, each  $10^\circ$  wide, azimuth ( $Az$ ) was divided into 8 intervals, each  $45^\circ$  and GDOP value ( $w$ ) into 8 intervals:  $w < 2$ ,  $2 \leq w < 3$ ,  $3 \leq w < 4$ ,  $4 \leq w < 5$ ,  $5 \leq w < 6$ ,  $6 \leq w < 8$ ,  $8 \leq w < 20$  and  $w \geq 20$ .

**Table 2.** The lowest and the greatest number of satellites visible for different masking elevation angle ( $H_{\min}$ ) for GPS, GLONASS, Galileo and BeiDou systems at different observer's latitudes ( $\varphi$ )

Latitude [ $^\circ$ ]	System	$H_{\min}$					
		$0^\circ$	$5^\circ$	$10^\circ$	$15^\circ$	$20^\circ$	$25^\circ$
0 – 10	GPS	9 – 13	7 – 13	6 – 12	5 – 10	4 – 9	3 – 8
	GLONASS	7 – 12	5 – 11	5 – 8	4 – 8	3 – 7	2 – 6
	Galileo	11 – 14	10 – 13	8 – 12	6 – 11	4 – 10	4 – 9
	BeiDou	9 – 12	8 – 12	7 – 10	5 – 10	4 – 8	4 – 7
10 – 20	GPS	8 – 13	6 – 12	5 – 11	4 – 10	3 – 9	3 – 8
	GLONASS	6 – 11	5 – 10	4 – 9	4 – 8	3 – 7	2 – 7
	Galileo	10 – 13	8 – 13	7 – 12	6 – 12	4 – 11	4 – 9
	BeiDou	8 – 12	6 – 12	6 – 10	5 – 9	4 – 9	4 – 8
20 – 30	GPS	7 – 13	6 – 12	5 – 11	4 – 10	3 – 9	3 – 8
	GLONASS	6 – 12	5 – 10	4 – 10	4 – 9	3 – 8	3 – 7
	Galileo	8 – 14	8 – 12	6 – 12	6 – 11	4 – 11	4 – 9
	BeiDou	6 – 12	6 – 11	6 – 10	5 – 9	4 – 9	4 – 7
30 – 40	GPS	7 – 13	6 – 13	5 – 10	4 – 9	3 – 9	3 – 7
	GLONASS	6 – 12	6 – 11	4 – 10	4 – 9	4 – 8	3 – 7
	Galileo	8 – 13	8 – 12	6 – 12	6 – 10	5 – 11	4 – 9
	BeiDou	7 – 12	6 – 12	6 – 10	5 – 9	5 – 9	4 – 7
40 – 50	GPS	7 – 13	6 – 12	5 – 11	4 – 9	3 – 9	3 – 8
	GLONASS	7 – 11	5 – 11	4 – 10	4 – 9	4 – 8	4 – 7
	Galileo	8 – 14	8 – 12	6 – 12	6 – 11	4 – 11	4 – 9
	BeiDou	7 – 12	6 – 12	6 – 10	5 – 10	4 – 8	4 – 7
50 – 60	GPS	8 – 13	6 – 12	5 – 11	4 – 10	3 – 9	3 – 8
	GLONASS	8 – 12	7 – 11	5 – 10	4 – 9	4 – 8	4 – 7
	Galileo	9 – 14	8 – 13	6 – 12	6 – 11	4 – 11	4 – 9
	BeiDou	8 – 12	6 – 11	6 – 10	5 – 10	4 – 9	4 – 7
60 – 70	GPS	8 – 14	6 – 13	5 – 12	4 – 11	3 – 9	3 – 8
	GLONASS	8 – 12	7 – 11	6 – 10	5 – 9	5 – 9	4 – 8
	Galileo	11 – 14	9 – 12	7 – 12	6 – 10	5 – 10	4 – 9
	BeiDou	9 – 12	8 – 12	7 – 11	6 – 9	5 – 9	4 – 7
70 – 80	GPS	8 – 14	6 – 13	6 – 12	5 – 11	4 – 10	3 – 9
	GLONASS	8 – 12	7 – 11	6 – 10	6 – 9	5 – 9	4 – 8
	Galileo	11 – 14	9 – 12	9 – 12	8 – 11	5 – 11	4 – 9
	BeiDou	9 – 12	8 – 12	8 – 11	6 – 9	5 – 8	4 – 8
80 – 90	GPS	8 – 14	8 – 12	7 – 12	6 – 11	4 – 10	4 – 9
	GLONASS	9 – 12	8 – 11	6 – 10	6 – 9	6 – 9	4 – 8
	Galileo	12 – 14	10 – 12	9 – 12	8 – 11	6 – 10	6 – 9
	BeiDou	9 – 12	9 – 12	8 – 10	7 – 9	6 – 9	4 – 8

### 3. VISIBILITY OF SATELLITES

The lowest ( $Is_{\min}$ ) and the greatest ( $Is_{\max}$ ) number  $Is$  of GPS, GLONASS, Galileo and BeiDou MEO satellites visible by the observer in open area above different  $H_{\min}$  in all 9 zones of latitudes are presented in Table 2. The numbers  $Is_{\min}$  and  $Is_{\max}$  depend on the SNS, angle  $H_{\min}$  and zone of latitudes. Additionally we can say that:

- for  $H_{\min} = 0^\circ$  the greatest number of  $l_{s_{\max}}$  is equal 14, Galileo in zone  $0 \div 10^\circ$  and at latitudes  $40 \div 90^\circ$  and GPS at latitudes  $60 \div 90^\circ$ ; the lowest number of  $l_{s_{\min}}$  is equal 6, GLONASS at latitudes  $10 \div 40^\circ$ ;
- if  $H_{\min} \leq 15^\circ$  the position 3D ( $l_{s_{\min}} \geq 4$ ) can be obtained by all four SNSs in all 9 zones, if  $H_{\min} = 20^\circ$  or  $25^\circ$  by Galileo and BeiDou only;
- if  $H_{\min} \leq 20^\circ$  the position 2D ( $l_{s_{\min}} \geq 3$ ) can be obtained by all four SNSs in all 9 zones, if  $H_{\min} = 25^\circ$  also but except for GLONASS at latitudes  $0 \div 20^\circ$  ( $l_{s_{\min}} = 2$ );
- at given  $H_{\min}$  in most of cases the numbers  $l_{s_{\min}}$  and  $l_{s_{\max}}$  are at low latitudes ( $0 \div 20^\circ$ ) lower than at high latitudes ( $70 \div 90^\circ$ ) for all 4 SNSs;
- total number of satellites for GPS and BeiDou taken into account in calculations is the same (27), but for  $H_{\min} \leq 10^\circ$  in most of cases  $l_{s_{\min}}$  is for GPS equal or less than for BeiDou while  $l_{s_{\max}}$  is for GPS greater or equal than for BeiDou. For  $H_{\min} \geq 20^\circ$   $l_{s_{\min}}$  is for GPS greater than 3 in zone  $80 \div 90^\circ$  only while in the case of BeiDou which orbit is 1317 km higher than for GPS orbit (tab.1) in all 9 zones;
- the  $l_{s_{\min}}$  (12) and  $l_{s_{\max}}$  (14) are the greatest in the case of Galileo both for  $H_{\min} = 0^\circ$  (zone  $80-90^\circ$ ) however for  $H_{\min} = 0^\circ$  and at latitudes  $60-90^\circ$  the  $l_{s_{\max}}$  is for Galileo and GPS the same (14). It is possible even though the total number of GPS satellite (27) is less than the total number of Galileo satellites (30) but American satellites are not evenly distributed on the orbits;
- the differences of  $l_{s_{\max}}$  and  $l_{s_{\min}}$  for  $H_{\min} = 0^\circ$  and  $H_{\min} = 25^\circ$  are in most of cases for all four SNSs equal both 4, 5 or 6. The greatest difference (7) is for Galileo in zone  $0-20^\circ$ ;
- the biggest difference (5) of  $l_{s_{\min}}$  in one zone is for  $H_{\min} = 5^\circ$  at latitude  $0-10^\circ$  (Galileo 10, GLONASS 5);
- at latitudes  $40-80^\circ$  for  $H_{\min} \geq 20^\circ$  the  $l_{s_{\min}}$  is the same for GLONASS and Galileo (5 or 4) despite Galileo spatial segment consists of 30 satellites while GLONASS of 24 only.

If the number  $l_s$  is equal 4 the user must be very careful because the number of satellites which can be used in 3D position determination can decrease at any moment and for any reason. That's why the additional calculations were made for each SNS for different  $H_{\min}$  in order to determine the greatest elevation  $H_{\max4}$  and  $H_{\max3}$  for which the number  $l_s$  of satellites visible at different latitudes in open area above this angle is equal 4 (minimum for position 3D) or 3 (minimum for position 2D), respectively (Table 3). We can remark that:

- the elevation  $H_{\max4}$  is lower considerably than  $H_{\max3}$  always in all 9 zones for all 4 SNSs;
- the difference between  $H_{\max4}$  and  $H_{\max3}$  depends on the latitude zone and SNS (the total number of satellites and their distribution, orbit altitude and its inclination, in particular), the greatest (10) and the lowest (1) values of this difference are for GLONASS in zone  $20-30^\circ$  and for BeiDou and for Galileo in zone  $80-90^\circ$ , respectively;
- comparing the results for different SNSs the elevation  $H_{\max4}$  is in each zone the greatest for Galileo, in the case of  $H_{\max3}$  also except the zone  $80-90^\circ$  where maximum is for GLONASS (its orbit inclination is nearly  $10^\circ$  higher than for Galileo);
- at low latitudes  $0-20^\circ$  elevations  $H_{\max4}$  and  $H_{\max3}$  are for GLONASS lower or equal elevations for GPS, but at latitudes  $40-90^\circ$  both elevations are for GLONASS greater than for GPS. It is the result of higher orbit inclination of Russian system in spite of lower orbit altitude and lower number of satellites;
- the greatest difference of  $H_{\max4}$  and  $H_{\max3}$  in one zone is equal 11 at latitude  $20-30^\circ$  (BeiDou – 29, GLONASS – 18) and 10 at latitude  $80-90^\circ$  (GLONASS – 40, GPS – 30), respectively.

**Table 3.** The GPS, GLONASS, Galileo and BeiDou systems, the greatest elevation  $H$  [°],  $H_{\max 4}$  and  $H_{\max 3}$ , for which the number  $l_s$  of satellites visible at different latitudes by the observer in open area above this angle is equal 4 or 3, respectively

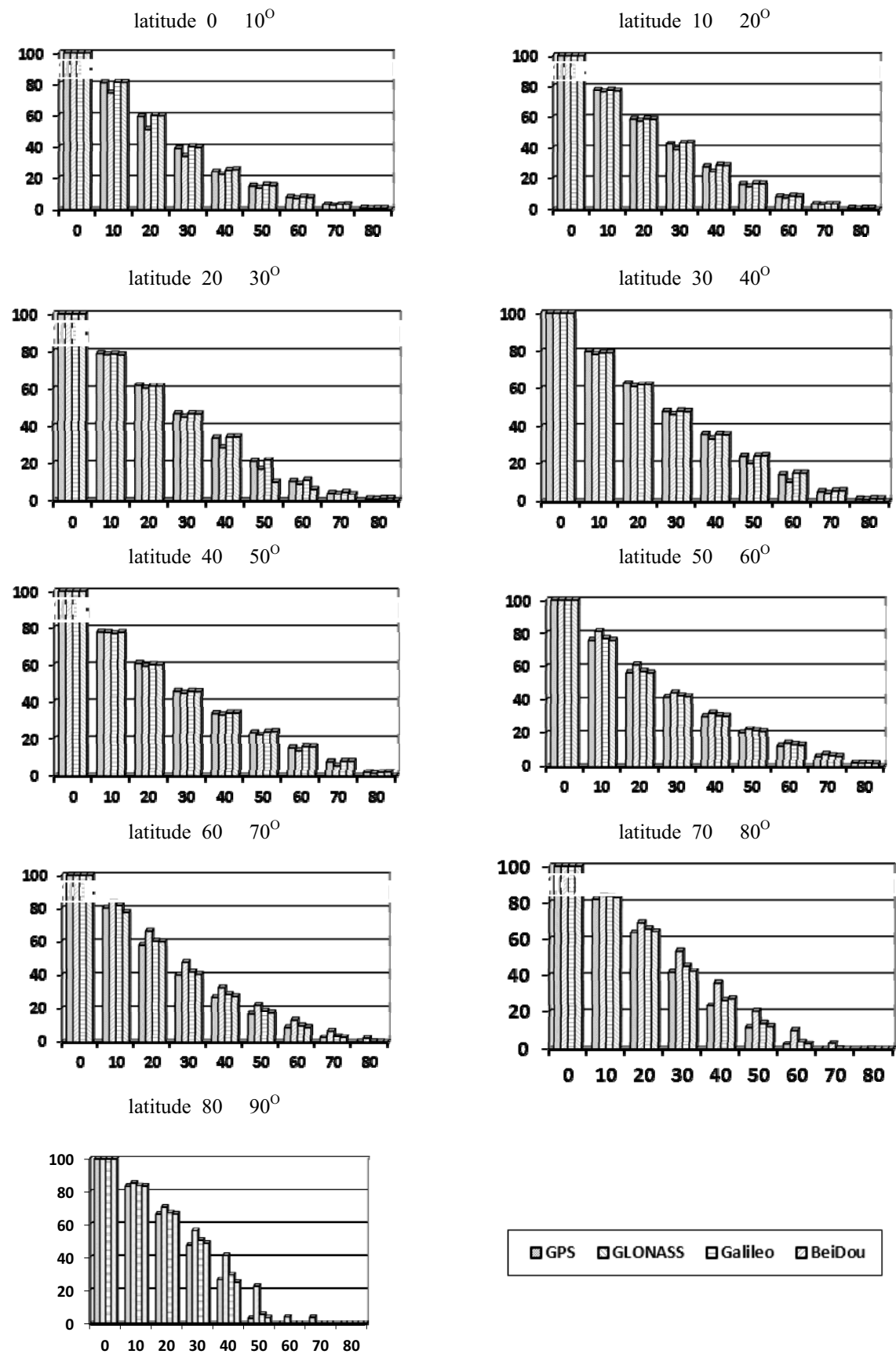
Latitude [°]	System	Number $l_s$ of satellites					
		4	3				
0 – 10	GPS	20	25	40 – 50	GPS	19	27
	GLONASS	15	22		GLONASS	25	28
	Galileo	27	33		Galileo	29	34
	BeiDou	25	32		BeiDou	28	33
10 – 20	GPS	19	25	50 – 60	GPS	18	26
	GLONASS	19	24		GLONASS	25	33
	Galileo	29	34		Galileo	27	34
	BeiDou	27	33		BeiDou	25	32
20 – 30	GPS	19	26	60 – 70	GPS	18	27
	GLONASS	18	28		GLONASS	27	30
	Galileo	30	35		Galileo	28	35
	BeiDou	29	35		BeiDou	26	32
30 – 40	GPS	18	27	70 – 80	GPS	22	27
	GLONASS	23	27		GLONASS	30	32
	Galileo	29	34		Galileo	31	35
	BeiDou	28	33		BeiDou	30	32
	GPS			80 – 90	GPS	26	30
	GLONASS				GLONASS	32	40
	Galileo				Galileo	35	36
	BeiDou				BeiDou	33	34

#### 4. SATELLITE ELEVATION AND AZIMUTH

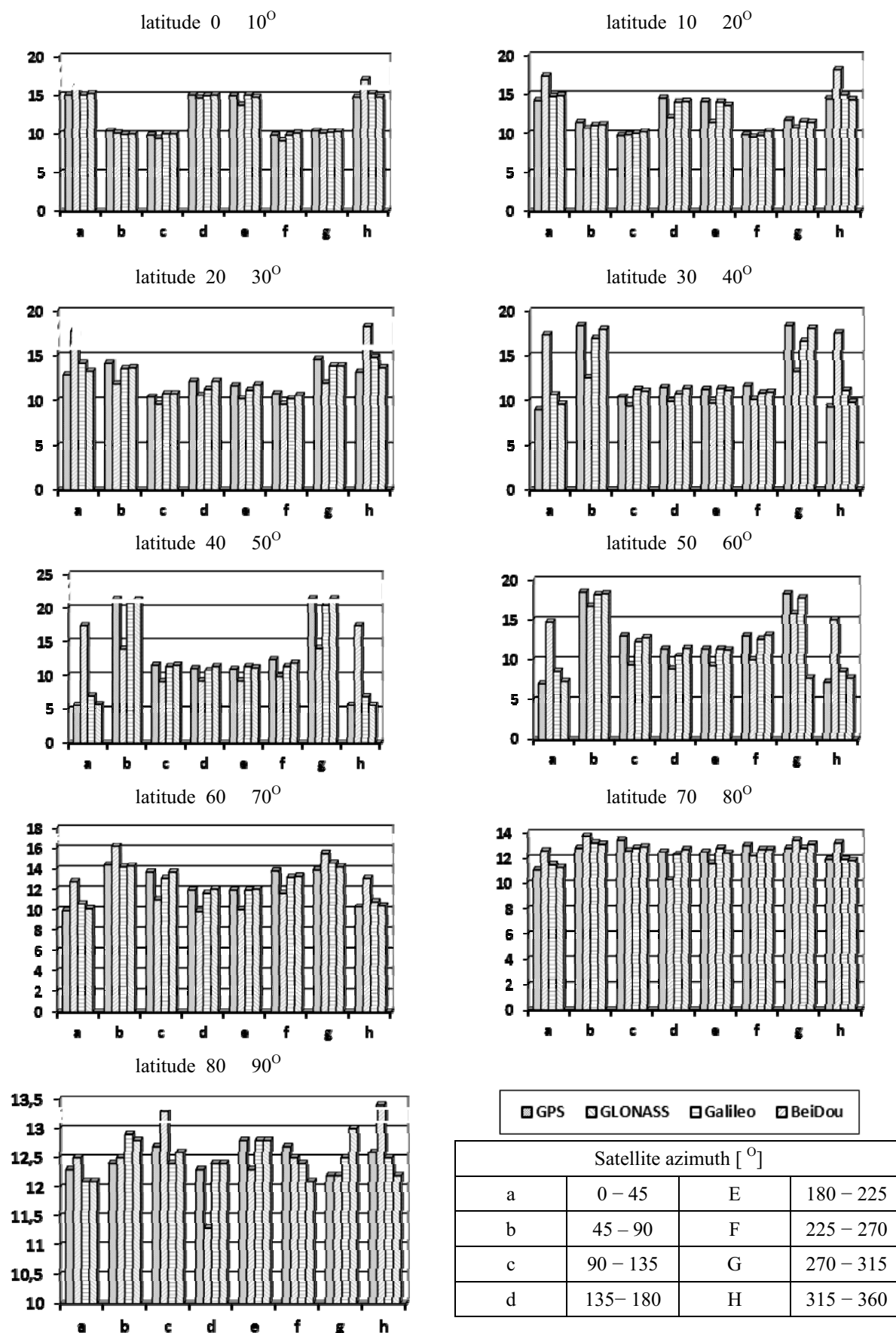
Percentage of MEO satellites visible by the observer in open area above elevation angle  $H$  in all 9 latitude zones for all four SNSs is showed in Figure 1. Additionally the weighted mean number of satellites  $l_{sm}$  visible above horizon ( $H = 0^\circ$ ) for each SNS in each zone was calculated. We can say that:

- the number  $l_{sm}$  is in all 9 zones the greatest and the lowest in the case of Galileo and GLONASS respectively;
- the percentage of satellites visible decreases with angle  $H$  in each zone for all SNSs, if this angle is equal  $20^\circ$  this percentage decreases to about 60% or more, if it is  $40^\circ$  to about 30% or more;
- for three SNSs, GPS, Galileo and BeiDou, the percentage of satellites visible is for each  $H$  in all zones almost the same. In the case of GLONASS this percentage differs, in zone  $0-10^\circ$  and at latitudes  $50-90^\circ$ , in particular;
- because of orbit inclination value ( $55^\circ$  or  $56^\circ$ ) and geometrical figure of the Earth the GPS, Galileo and BeiDou MEO satellites in the zones  $70-80^\circ$  and  $80-90^\circ$  cannot be visible above  $70^\circ$  and approximately  $57^\circ$  respectively. In the case of GLONASS because of its orbit inclination ( $64.8^\circ$ ) the satellites can be visible in zone  $70-80^\circ$  above  $80^\circ$  and in zone  $80-90^\circ$  above  $60^\circ$ ;
- for each SNS elevation angle  $H$  can be equal  $90^\circ$  (satellite in zenith) but only at latitudes lower than given SNS inclination (GPS and BeiDou  $55^\circ$ , Galileo  $56^\circ$ , GLONASS  $64.8^\circ$ ). That's why in Poland, north part in particular (e.g. latitude of Gdynia  $54^\circ 30'$ ) the GPS satellites are visible in zenith very rarely.

As the satellite azimuth depends on the user's latitude and angle  $H_{\min}$  the calculations for all four SNSs were made for all 9 zones of latitudes and for different masking elevation angle.



**Fig. 1.** Percentage of GPS, GLONASS, Galileo and BeiDou MEO satellites visible in open area above angle ( $H$ ) at different observer's latitudes ( $\varphi$ )



**Fig. 2.** Distribution (in per cent) of GPS, GLONASS, Galileo and BeiDou MEO satellites azimuths in open area at different observer's latitudes ( $\varphi$ ),  $H_{\min} = 5^\circ$

The distributions of satellite azimuths for open area for the most frequently used angle  $H_{\min} = 5^\circ$  are presented in Figure 2. In the case of three SNSs, GPS, Galileo and BeiDou, we can resume that:

- as the orbit inclination of these systems is almost the same ( $55^\circ$  or  $56^\circ$ ) the distribution of satellites azimuths is for each system almost the same also;
- at latitudes  $70^\circ$ – $90^\circ$  the number of satellites in all 8 azimuths intervals is almost the same;
- at latitudes  $30^\circ$ – $60^\circ$  the number of satellites in azimuth interval  $045^\circ$ – $90^\circ$  and  $270^\circ$ – $315^\circ$  is greater than in all 6 other intervals considerably;
- at latitudes  $40^\circ$ – $60^\circ$  the number of satellites with azimuth  $315^\circ$ – $045^\circ$  is less than in all other intervals, adjacent intervals in particular.

In the case of GLONASS system we can say that:

- the distribution, except for zone  $80^\circ$ – $90^\circ$ , differs from the distribution of all three other SNS, in some zone considerably;
- at latitudes  $0^\circ$ – $20^\circ$  the number of satellites with azimuths from intervals  $045^\circ$ – $135^\circ$  and  $225^\circ$ – $315^\circ$  is for  $H_{\min} = 5^\circ$  less than in all other intervals;
- at latitudes  $40^\circ$ – $60^\circ$  the greatest number of satellites is interval  $315^\circ$ – $045^\circ$  while in this interval the number of GPS, Galileo and BeiDou satellites is the lowest.

## 5. GDOP COEFFICIENT VALUE

Distribution (in per cent) of GDOP coefficient values in open area for all 4 SNSs for  $H_{\min} = 5^\circ$  in all 9 latitudes zones is presented in Figure 3. We can say that:

- for each SNS distribution of GDOP values depends on observer's latitude and angle  $H_{\min}$ ;
- for all SNSs GDOP value is at latitudes  $70^\circ$ – $90^\circ$  greater than at latitudes  $0^\circ$ – $70^\circ$ , in zone  $80^\circ$ – $90^\circ$  in particular;
- distribution for GLONASS system differs from the distributions for other 3 SNSs, at latitudes  $20^\circ$ – $40^\circ$  in particular;
- in zone  $80^\circ$ – $90^\circ$  GDOP value is for all SNSs equal at least 4, in approximately 20% it is greater than 20;
- GDOP value can be less than 2 but in the case of GPS, Galileo and BeiDou at latitudes  $0^\circ$ – $20^\circ$  only;
- at latitudes  $0^\circ$ – $60^\circ$  for all SNSs GDOP value is in most cases less than 3 except for GLONASS system at latitudes  $20^\circ$ – $40^\circ$ ;
- at latitudes  $0^\circ$ – $70^\circ$  for all SNSs GDOP value is less than 5, except for GPS system in zone  $60^\circ$ – $70^\circ$ .

The additional calculations were made in zone  $50^\circ$ – $60^\circ$  for the same SNSs for other  $H_{\min}$  values ( $0^\circ$ ,  $10^\circ$ ,  $15^\circ$ ,  $20^\circ$  and  $25^\circ$ ). The results are showed in Figure 4. We can state that:

- for all four SNSs GDOP value increases with  $H_{\min}$ , the greatest increase is between  $10^\circ$  and  $15^\circ$ ;
- if  $H_{\min} \leq 20^\circ$  the distributions of GDOP values is for all four SNSs almost the same however if  $10^\circ \leq H_{\min} \leq 15^\circ$  the greatest values of GDOP for Galileo and BeiDou systems are less than for GPS and GLONASS systems;
- if  $H_{\min} = 25^\circ$  GDOP values for GLONASS systems are greater than for other 3 SNSs considerably;
- if  $H_{\min} \leq 5^\circ$  GDOP value is for GLONASS and Galileo systems less than 4 and for GPS and BeiDou systems less than 5. If  $H_{\min} = 25^\circ$  this value is for all SNSs greater than 3.



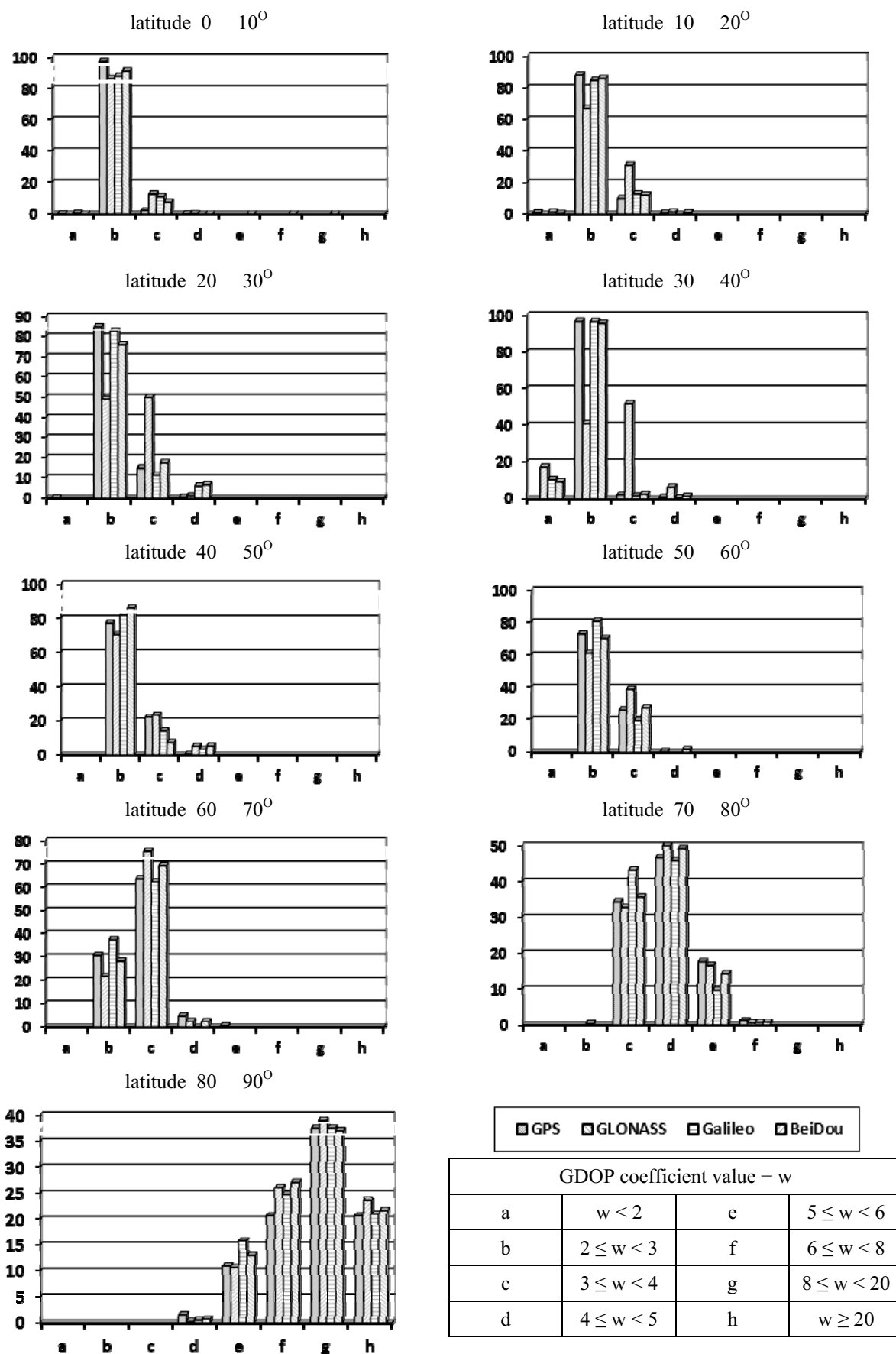
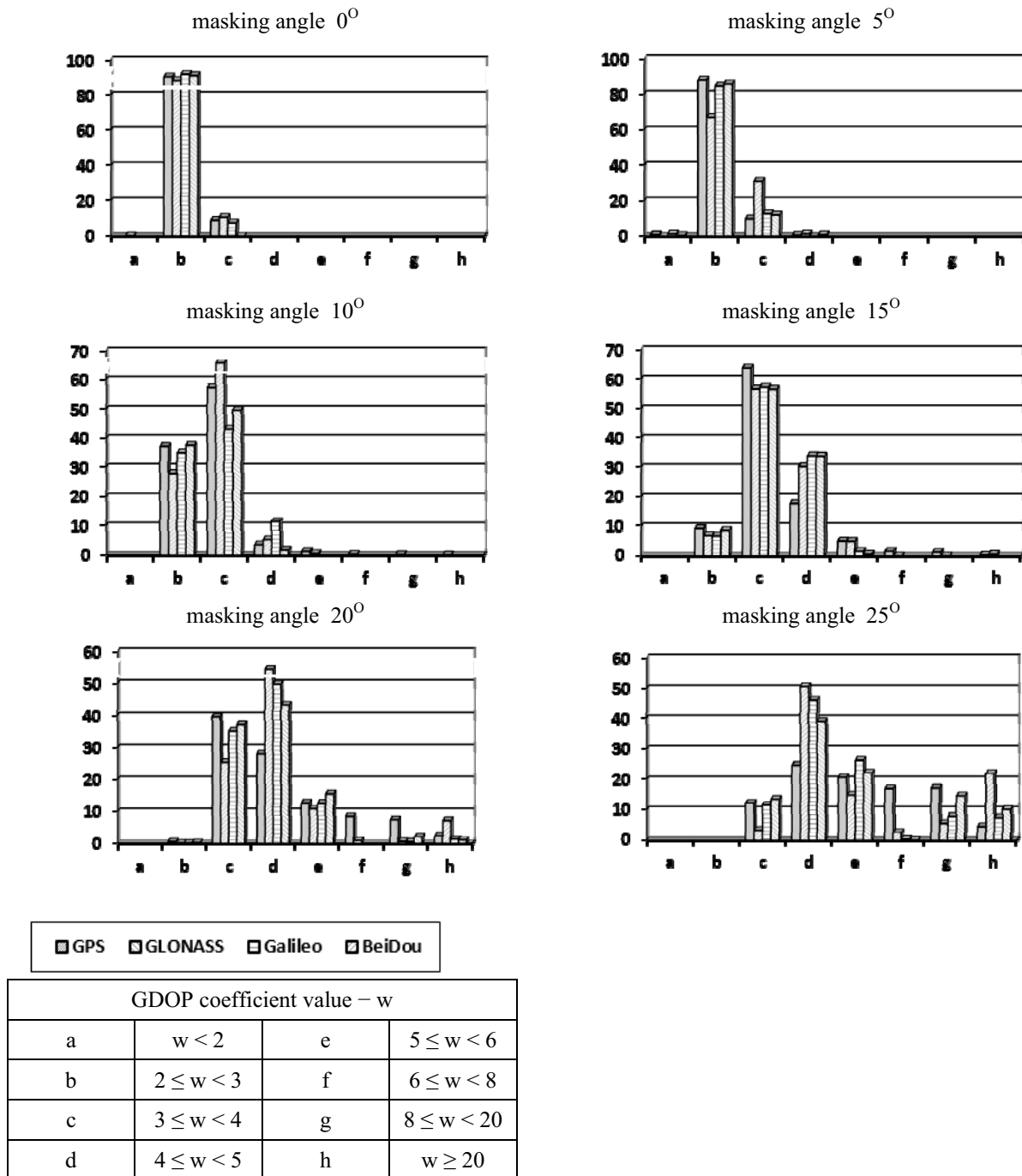


Fig. 3. GPS, GLONASS, Galileo and BeiDou systems, distribution (in per cent) of GDOP coefficient values for masking elevation angle  $H_{\min} = 5^\circ$  at different observer's latitudes ( $\varphi$ )



**Fig. 4.** GPS, GLONASS, Galileo and BeiDou systems, distribution (in per cent) of GDOP coefficient values for different masking elevation angles at observer's latitudes  $50 - 60^\circ$

Distribution (in per cent) of GDOP coefficient values for the observer at latitudes  $50 - 60^\circ$ , if the number of visible satellites  $l_s$  is known, for  $H_{\min} = 5^\circ$  is presented in Table 4. We can notice that there is not a direct relation between a number  $l_s$  of satellites visible above  $H_{\min}$  and GDOP coefficient value, but we can realize "when  $l_s$  is greater, GDOP can be less" and vice versa "when  $l_s$  is less, GDOP can be greater". We can observe also that GDOP coefficient value for:

- all four SNSs is from interval  $[2, 4]$  if  $l_s$  is equal 8, 9 or 10;
- GPS and BeiDou systems is from interval  $[3, 5]$  if  $l_s$  is equal 6;
- GPS, GLONASS and BeiDou systems is from interval  $[3, 4]$  if  $l_s$  is equal 7;
- GPS system is less than 3 if  $l_s$  is equal 11 or 12.

**Table 4.** Distribution (in per cent) of GDOP coefficient values at observer's latitudes  $50^{\circ}$ – $60^{\circ}$   $H_{\min} = 5^{\circ}$ , if the number of visible satellites  $l_s$  is known

Visible satellites			GDOP coefficient value – w		
$l_s$	System	%	$2 \leq w < 3$	$3 \leq w < 4$	$4 \leq w < 5$
6	GPS	0.6		0.2	0.4
	GLONASS	–	–	–	–
	Galileo	–	–	–	–
	BeiDou	2.1	–	0.3	1.8
7	GPS	3.8		3.8	
	GLONASS	1.0		1.0	
	Galileo	–	–	–	–
	BeiDou	3.5	–	3.5	–
8	GPS	14.5	3.6	10.9	
	GLONASS	38.5	9.2	29.3	
	Galileo	6.6	0.5	6.1	–
	BeiDou	14.9	3.3	11.6	–
9	GPS	27.8	17.0	10.8	
	GLONASS	51.2	42.8	8.4	
	Galileo	8.5	5.6	2.9	–
	BeiDou	28.1	16.8	11.3	–
10	GPS	46.0		45.2	0.8
	GLONASS	9.2		8.8	0.4
	Galileo	35.1		35.1	10.0
	BeiDou	45.0		43.9	1.1
11	GPS	7.1		7.1	
	GLONASS	–		–	–
	Galileo	38.2		36.9	0.3
	BeiDou	6.4		6.4	–
12	GPS	0.2		0.2	
	GLONASS	–		–	–
	Galileo	11.3		11.3	–
	BeiDou	–		–	–
13	GPS	–		–	–
	GLONASS	–		–	–
	Galileo	0.3		0.3	–
	BeiDou	–		–	–
X	GPS	100		73.1	26.5
	GLONASS	100		61.3	38.7
	Galileo	100		80.7	19.3
	BeiDou	100		70.4	27.8

## 6. CONCLUSIONS

- as in the case of GPS, Galileo and BeiDou orbit inclination and its altitude are almost the same and therefore the percentage of satellites visible above given angle and the distributions of satellite azimuths are almost the same also the most important for many users is the number of operational satellites. When this number is greater, DOP coefficients values can be less;
- GLONASS system with the lowest number of satellites (24 only) is and can be in the future thanks to orbit inclination ( $64.8^{\circ}$ ) useful especially for the users of area transport at high latitudes;
- the results of comparison between 27 BeiDou constellation (final number of MEO satellites) and GPS constellation with the same number of satellites showed that the visibility parameters and geometry are for both systems almost the same. It means explicitly that at the moment of FOC of BeiDou the users will have at least three SNSs (GPS, GLONASS and BeiDou) to choose from. The best system for all users will be certainly GPS system with the biggest number of satellites. BeiDou system can be back up system only;
- Full Operational Capability (FOC) of BeiDou system (2017 or later) will made China the third nation in possession of independent, global navigation system following the United States and Russia, however the interest in this system among satellite navigation systems users in the world will be little. D2 navigation message transmitted via 5 BeiDou GEO satellites will provide augmentation service information to the users but in China and Asia-Pacific region only. It means that integrity information will be not accessible to users in Europe, in Poland also.

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